# ${ }^{17}$ O NMR Study of Chromium(VI) Ions in Water 

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#### Abstract

A mathematical model for oxygen exchange out of labeled (e.g., ${ }^{17} \mathrm{O}$ ) $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ into solvent $\mathrm{H}_{2} \mathrm{O}$ according to the dimerization reaction $2 \mathrm{CrO}_{4}{ }^{2-}+2 \mathrm{H}^{+} \rightleftharpoons\left(1 / K_{\mathrm{a}\left(\mathrm{HCrO}_{4}-\right)}\right) 2 \mathrm{HCrO}_{4}^{-} \rightleftharpoons(\alpha / \beta) \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}+\mathrm{H}_{2} \mathrm{O}$ is described. Two rates of isotopic change are identified: (1) a rapid change intimately associated with the attainment of chemical equilibrium, but not identical with it (rate constants $v_{1}$ and $v_{2}$, respectively), in which the fractional label in monomeric $\mathrm{HCrO}_{4}{ }^{-}+\mathrm{CrO}_{4}{ }^{2-}(p)$ decreases more rapidly than that in the dimer $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(q)$, i.e. $\dot{p}>\dot{q}$, followed by (2) a slower decrease in both ( $\dot{q}>\dot{p}$ ) until isotopic equilibrium with the solvent is established, $p=q=r$ (rate constant $\nu_{3}$ ). Visible-UV and ${ }^{17} \mathrm{O}$ NMR spectra have been used to characterize the elusive $\mathrm{HCrO}_{4}^{-}$ion. Vibrational fine structure is seen in the visible spectrum ( $C_{3 v}$ symmetry), and integration of the monomeric $\left(\mathrm{HCrO}_{4}^{-}+\mathrm{CrO}_{4}{ }^{2-}\right){ }^{17} \mathrm{O}$ absorption agrees with only four O atoms in $\mathrm{HCrO}_{4}{ }^{-}$. A pH-dependent shift to higher frequency $\left(\delta_{\mathrm{CrO}_{4}}{ }^{2-}=812\right.$ $\left.\mathrm{ppm} ; \delta_{\mathrm{HCrO}_{4}}=860 \mathrm{ppm}\right)$ is used to give $\left.\mathrm{p} K_{\mathrm{a}\left(\mathrm{HCrO}_{4}-\right.}\right)=5.80\left(I=1.0 \mathrm{M}, 25^{\circ} \mathrm{C}\right)$, and comparisons with the integrated  6.0 M ), at $25^{\circ} \mathrm{C}$. Dimerization and hydrolytic rate constants ( $\alpha$ and $\beta$ ) have been obtained under the conditions of the ${ }^{17} \mathrm{O}$ exchange experiments; they are shown to contain spontaneous, buffer, and $\left[\mathrm{H}^{+}\right]$and $\left[\mathrm{OH}^{-}\right]$contributions in agreement with earlier investigations. ${ }^{17} \mathrm{O}$ exchange out of enriched $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ has been followed in aqueous solutions over the concentration range $0.01-2.0 \mathrm{M}$ and over the pH range $6.38-13.0$ at $25^{\circ} \mathrm{C}$ and constant ionic strength ( $I$ $=1.0,6.0$ ). The dimerization reaction (eq 1) contributes only at the highest $\mathrm{Cr}(\mathrm{VI})$ concentration ( 2.0 M ), and then only slightly (i.e., $\sim 10 \%$ at pH 7.3 ). The rate data have been interpreted in terms of the direct exchange paths $\mathrm{Cr}^{17} \mathrm{O}_{4}{ }^{2-}+\mathrm{H}_{2} \mathrm{O} \rightarrow\left(k_{1}\right) \mathrm{Cr}^{17} \mathrm{O}_{3} \mathrm{O}^{2-}+\mathrm{H}_{2}{ }^{17} \mathrm{O} ; \mathrm{HCr}^{17} \mathrm{O}_{4}^{-}+\mathrm{H}_{2} \mathrm{O} \rightarrow\left(k_{2}\right) \mathrm{HCr}^{17} \mathrm{O}_{3} \mathrm{O}^{-}+\mathrm{H}_{2}{ }^{17} \mathrm{O} ; \mathrm{H}_{2} \mathrm{Cr}^{17} \mathrm{O}_{4}+\mathrm{H}_{2} \mathrm{O} \rightarrow$ $\left(k_{3}\right) \mathrm{H}_{2} \mathrm{Cr}^{17} \mathrm{O}_{3} \mathrm{O}+\mathrm{H}_{2}{ }^{17} \mathrm{O} ; \mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{7}{ }^{2-}+\mathrm{H}_{2} \mathrm{O} \rightarrow\left(k_{4}\right) \mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{6} \mathrm{O}^{2-}+\mathrm{H}_{2}{ }^{17} \mathrm{O}$, with rate constants $k_{1}=7.2 \times 10^{-8} \mathrm{M}^{-1}$ $\mathrm{s}^{-1}, k_{2}=7.6 \times 10^{-4} \mathrm{M}^{-1} \mathrm{~s}^{-1}, k_{3}=1.7 \times 10^{5} \mathrm{M}^{-1} \mathrm{~s}^{-1}\left(I=1.0 \mathrm{M}, 25^{\circ} \mathrm{C}\right)$, and $k_{4}=4.1 \times 10^{-3} \mathrm{M}^{-1} \mathrm{~s}^{-1}(I=6.0$ $\mathrm{M}, 25^{\circ} \mathrm{C}$ ). The monomeric paths (but not the rate constants) agree with those found in an earlier study, but that involving $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ is new. Rate constants for ${ }^{17} \mathrm{O}$ exchange are compared with those of other substitution reactions of $\mathrm{HCrO}_{4}^{-}$and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$.


## Introduction

We have become interested in $\mathrm{Cr}(\mathrm{VI})$ as it applies to its mutagenic and carcinogenic properties. ${ }^{1}$ It is likely, in our view, that oxidation of thiolic substrates begins with substitution at the $\mathrm{Cr}(\mathrm{VI})$ center so that the O lability of $\mathrm{Cr}(\mathrm{VI})$ species in aqueous solution is important to establish. The rates and mechanisms of O exchange between water and $\mathrm{CrO}_{4}{ }^{2-}, \mathrm{HCrO}_{4}^{-}$, $\mathrm{H}_{2} \mathrm{CrO}_{4}$, and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ remain uncertain or unknown. ${ }^{2}$ There have been six previous studies, most making use of ${ }^{18} \mathrm{O}$ tracers. Some comment on these is appropriate.

Mills ${ }^{3}$ developed an ingenious method for following exchange from isotopically normal $\mathrm{Cr}(\mathrm{VI})$ species into ${ }^{18} \mathrm{O}$-depleted $\mathrm{H}_{2} \mathrm{O}$, whereby he measured the solvent ${ }^{18} \mathrm{O}$ content by timing the fall of drops of $\mathrm{H}_{2} \mathrm{O}$ distillate through $m$-fluorotoluene maintained at constant temperature $\left(19.33{ }^{\circ} \mathrm{C}\right)$. Very high $\mathrm{Cr}(\mathrm{VI})$ concentrations were used ( $2.1-5.4 \mathrm{M}$ ). Exchange was found to be complete in the time of the first analysis with $\mathrm{CrO}_{3}$ and more rapid than could be estimated using known rate constants for the dimerization-hydrolysis reaction

$$
\begin{equation*}
2 \mathrm{HCr}^{17} \mathrm{O}_{4} \stackrel{-\alpha}{\underset{\beta}{\rightleftarrows}} \mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{7}{ }^{2-}+\mathrm{H}_{2}{ }^{17} \mathrm{O} \tag{1}
\end{equation*}
$$

when $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ was used. Mills suggested ${ }^{4}$ that dissociative

[^0]dehydration of $\mathrm{H}_{2} \mathrm{CrO}_{4}$ was responsible, viz.
\[

$$
\begin{equation*}
\mathrm{HCr}^{17} \mathrm{O}_{4}^{-}+\mathrm{H}^{+} \rightleftharpoons \mathrm{H}_{2} \mathrm{Cr}^{17} \mathrm{O}_{4} \rightleftarrows \mathrm{Cr}^{17} \mathrm{O}_{3}+\mathrm{H}_{2}^{17} \mathrm{O} \tag{2}
\end{equation*}
$$

\]

Subsequently, Baloga and Earley ${ }^{5}$ used ${ }^{18} \mathrm{O}$-enriched $\mathrm{Li}_{2} \mathrm{CrO}_{4}(2.68$ atom $\%$ ) and normal $\mathrm{H}_{2} \mathrm{O}$ containing $\mathrm{HClO}_{4}$ or $\mathrm{LiOH}(I=1.0 \mathrm{M})$. Exchange was monitored by mass spectrometric analysis of $\mathrm{O}_{2}$ liberated by heating $\mathrm{BaCrO}_{4}$ recovered from the reaction mixture following addition of $\mathrm{Ba}^{2+}$ at various times. Much lower $\mathrm{Cr}(\mathrm{VI})$ concentrations were used ( $0.014-0.3 \mathrm{M}$ ), and it was found that exchange into $\mathrm{CrO}_{4}{ }^{2-}$ was slow ( $1.2 \times 10^{-5} \mathrm{~s}^{-1}$ at $25^{\circ} \mathrm{C}$ ) and $\mathrm{Cr}(\mathrm{VI})$ concentration independent. At pH 7.20 , exchange was faster with a second-order dependence on $[\mathrm{Cr}(\mathrm{VI})]$. This latter exchange was attributed to a $k_{\mathrm{D}}\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right]$ term in the rate law, with $k_{\mathrm{D}}$ being equated with the hydrolysis rate constant $\beta$ of eq 1 . At $\operatorname{Cr}(\mathrm{VI})$ concentrations greater than $\sim 0.1 \mathrm{M}$ an additional higher-order term in $[\mathrm{Cr}(\mathrm{VI})]$ was also noted. Holyer and Baldwin ${ }^{6}$ examined in detail this higher concentration condition ( $1.0-2.68 \mathrm{M}$ ), again using $\mathrm{H}_{2} \mathrm{O}$ distillates, but this time using mass spectrometric analysis of equilibrated $\mathrm{CO}_{2}$. They found a $[\mathrm{Cr}(\mathrm{VI})]$-independent rate $(7 \times$ $10^{-7} \mathrm{~s}^{-1}, 25^{\circ} \mathrm{C}$ ) in alkaline solution, and a second-order dependence on $[\mathrm{Cr}(\mathrm{VI})]$ with an approaching second-order dependence on $\left[\mathrm{H}^{+}\right]$ at $\mathrm{pH}<10$. This data was once again related to the equilibrium process of eq 1 , with the additional pathway

[^1]\[

$$
\begin{equation*}
\mathrm{HCr}^{17} \mathrm{O}_{4}^{--}+\mathrm{Cr}^{17} \mathrm{O}_{4}^{2-} \rightleftarrows \mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{7}^{2-}+{ }^{17} \mathrm{OH}^{-} \tag{3}
\end{equation*}
$$

\]

being used to take care of the less than second-order term in $\left[\mathrm{H}^{+}\right]$. Mak ${ }^{7}$ examined exchange in more acidic solution ( $\mathrm{pH} 4.5-8.4$ ) using a flow method to mix and then quench (as $\mathrm{BaCrO}_{4}$ ) the reactants. He found much faster rates (reaction times varied from 0.03 to 0.5 s ) with a second-order dependence on [ $\mathrm{Cr}(\mathrm{VI})]$ (at pH 8.4-7.0) turning into a third-order dependence as the acidity increased. No first-order term was found. The second-order term was assigned to dimerization as before, and the third-order term to the processes

$$
\begin{equation*}
\mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{7}{ }^{2-}+\mathrm{HCr}^{17} \mathrm{O}_{4}^{-} \rightleftharpoons \mathrm{Cr}_{3}{ }^{17} \mathrm{O}_{10}{ }^{2-}+{ }^{17} \mathrm{OH}^{-} \tag{4}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathrm{HCr}_{2}{ }^{17} \mathrm{O}_{7}^{-}+\mathrm{HCr}^{17} \mathrm{O}_{4}^{-} \rightleftarrows \mathrm{Cr}_{3}{ }^{17} \mathrm{O}_{10}{ }^{2-}+\mathrm{H}_{2}^{17} \mathrm{O} \tag{5}
\end{equation*}
$$

depending on reaction pH . Such processes bear some relationship to the much earlier ${ }^{17} \mathrm{O}$ line broadening study of Figgis, Kidd, and Nyholm ${ }^{8}(\sim 4 \mathrm{M}[\mathrm{Cr}(\mathrm{VI})])$, who suggested fast $\left(k=2.3 \times 10^{3}\right.$ $\mathrm{M}^{-1} \mathrm{~s}^{-1}, 27^{\circ} \mathrm{C}$ ) self-exchange between monomer and dimer in alkaline solution without involvement of solvent:

$$
\begin{equation*}
\mathrm{Cr}^{17} \mathrm{O}_{4}^{2-}+\mathrm{O}_{3} \mathrm{CrOCrO}_{3}{ }^{2-} \stackrel{k}{\rightleftarrows}{ }^{17} \mathrm{O}_{3} \mathrm{Cr}^{17} \mathrm{OCrO}_{3}^{2-}+\mathrm{CrO}_{4}^{2-} \tag{6}
\end{equation*}
$$

Finally, in the most recent study, where aqueous $\mathrm{Ba}^{2+}$ was used to precipitate $\mathrm{CrO}_{4}{ }^{2-}$, Okumura and co-workers ${ }^{9}$ found only a firstorder dependence on $[\mathrm{Cr}(\mathrm{VI})]$ at low concentrations ( $0.036-0.14$ M) irrespective of $\mathrm{pH}(12-7.2)$, which they attributed to the direct pathways 7-9. At higher concentrations (up to 0.96 M ), increasing

$$
\begin{gather*}
\mathrm{Cr}^{17} \mathrm{O}_{4}{ }^{2-}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Cr}^{17} \mathrm{O}_{3} \mathrm{O}^{2-}+\mathrm{H}_{2}{ }^{17} \mathrm{O}  \tag{7}\\
\mathrm{HCr}^{17} \mathrm{O}_{4}^{-}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{HCr}^{17} \mathrm{O}_{3} \mathrm{O}^{-}+\mathrm{H}_{2}{ }^{17} \mathrm{O}  \tag{8}\\
\mathrm{HCr}^{17} \mathrm{O}_{4}^{-}+\mathrm{H}^{+}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{HCr}^{17} \mathrm{O}_{3} \mathrm{O}^{-}+\mathrm{H}^{+}+\mathrm{H}_{2}{ }^{17} \mathrm{O} \tag{9}
\end{gather*}
$$

contributions from second-order, and higher-order, terms were found which they attributed to the dimerization processes of eqs 1 and 3 and to a $\mathrm{CrO}_{4}{ }^{2-}$-assisted general base catalyzed dimerization process. The direct pathways (eqs $7-9$ ) agree with Mills' early observations, ${ }^{3}$ but Okumura suggested, on the basis of a low activation energy ( $25.5 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ), that synchronous water displacement was responsible rather than hydration of the intermediate $\mathrm{CrO}_{3}$ species.

Overall, the above studies show discrepancies both in observed rates and in experimental rate laws. This may be due in part to the method of analysis. It has long been known that precipitation methods can lead to irregular and often spurious results. ${ }^{10}$ Indeed Okumura ${ }^{9}$ refers to precipitation-induced exchange into $\mathrm{BaCrO}_{4}$ at $\mathrm{pH}<8$. Furthermore, adjustment of solution pH to 9 immediately prior to precipitation necessarily involves additional exchange into any $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (by hydrolysis), and this becomes increasingly important as the $\mathrm{Cr}(\mathrm{VI})$ concentration increases. Distillation procedures also lead to isotopic fractionation. Clearly an in situ method of analysis is called for. But the dimerization process of eq 1 must lead to exchange,

[^2] 1967.
(8) Figgis, B. N.; Kidd, R. G.; Nyholm, R. S. Can. J. Chem. 1965, 43, 145.
(9) Okumura, M.; Kitani, M.; Toyomi Y.; Okazaki N. Bull. Chem. Soc. Jpn. 1980, 53, 3143.
(10) Anbar, M.; Gutman, S. Int. J. Appl. Radiat. Isot. 1959, 5, 23.
although the correct methodology for interpreting this for the various $\mathrm{Cr}(\mathrm{VI})$ species is not currently available. ${ }^{11,12}$

We decided to use ${ }^{17} \mathrm{O}$ NMR to follow exchange. ${ }^{13}$ This gives in situ detection, and the separate signals for $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (two types of O), $\mathrm{HCrO}_{4}^{-}+\mathrm{CrO}_{4}^{2-}$, and $\mathrm{H}_{2} \mathrm{O}^{14,15}$ allow a choice of reagent to follow. Also, the data can be readily analyzed for acidity $\left(K_{\mathrm{a}\left(\mathrm{HCO}_{4}^{-}\right)}^{-)}\right.$) and dimerization ( $K_{\mathrm{d}}$ ) constants. By using $40 \%{ }^{17} \mathrm{O}$-labeled $\mathrm{Cr}(\mathrm{VI})$, acceptable rate data can be obtained every 30 s or so (if necessary), and at low concentration ( 0.01 M).

## Results and Discussion

In part A of this section we set up the theory for exchange via dimerization; in part $B$ we give equilibrium and kinetic data which allow exchange via dimerization to be evaluated; and in part C we give our ${ }^{17} \mathrm{O}$ exchange data and discuss the mechanisms for exchange.
A. Oxygen Exchange via Dimerization. Mathematical models for exchange are available for both simple ${ }^{16}$ and complex ${ }^{17}$ oxyanion systems, but no treatment has been given for exchange via dimerization starting with an enriched substrate. The following treatment identifies two rate processes for a system initially not at equilibrium (i.e., such as when isotopically labeled $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ is dissolved in normal $\mathrm{H}_{2} \mathrm{O}$ ). The first is intimately associated with the attainment of chemical equilibrium, but is not identical with it, and differs for the various $\mathrm{Cr}(\mathrm{VI})$ species $\left(\mathrm{HCrO}_{4}{ }^{-}+\mathrm{CrO}_{4}{ }^{2-}, \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right)$ and $\mathrm{H}_{2} \mathrm{O}$. The second is the more gradual leakage of isotopic label out of the $\mathrm{Cr}(\mathrm{VI})$ species into $\mathrm{H}_{2} \mathrm{O}$.

A1. Reactions to Consider. When sodium chromate $\left(\mathrm{Na}_{2}-\right.$ $\mathrm{CrO}_{4}$ ), in which some of the oxygen atoms are isotopically labeled, is dissolved in water (which may also contain a label), equilibration with the solvent may occur via the processes

$$
2 \mathrm{Cr}^{17} \mathrm{O}_{4}^{2-}+2 \mathrm{H}^{+} \rightleftarrows 2 \mathrm{HCr}^{17} \mathrm{O}_{4}^{-} \rightleftarrows \mathrm{Cr}_{2}{ }^{17} \mathrm{O}_{7}{ }^{2-}+\mathrm{H}_{2}{ }^{17} \mathrm{O}
$$

For convenience this is coded

$$
\begin{equation*}
2 X_{1}+2 \mathrm{H}^{+} \rightleftarrows 2 X_{2} \underset{\beta^{\prime}}{\stackrel{\alpha^{\prime}}{\rightleftarrows}} Y+Z \tag{10}
\end{equation*}
$$

where, according to context, $X_{1}, X_{2}$, and $Y$ are either labels for, or concentrations of, $\mathrm{Cr}(\mathrm{VI})$ oxyanions; $Z$ similarly denotes water, and $\alpha^{\prime}$ and $\beta^{\prime}$ are rate constants. For measurements around neutrality, establishment of the $X_{1} / X_{2}$ equilibrium is fast ${ }^{18}$

[^3]compared to the $2 X_{2}$ gives $Y+Z$ reaction, so that
\[

$$
\begin{equation*}
X_{1}\left[\mathrm{H}^{+}\right] / X_{2}=\text { constant }=K_{\mathrm{a}} \tag{11}
\end{equation*}
$$

\]

$\left(\mathrm{p} K_{\mathrm{a}}=5.80,25.0^{\circ} \mathrm{C}, I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right)\right.$, cf. part B). In any given experiment the pH will also remain constant so that

$$
\begin{equation*}
X_{1}=\mu X_{2}, \quad \mu \equiv K_{\mathrm{a}} /\left[\mathrm{H}^{+}\right] \tag{12}
\end{equation*}
$$

The effect of chromate on the bichromate-dichromate reaction is therefore that of a buffer. Because of the rapidity of the $X_{1} /$ $X_{2}$ equilibrium, labeled O atoms belonging to these two species will appear together in the NMR spectrum, so that we may combine them into a single variable:

$$
\begin{equation*}
X=X_{1}+X_{2} \tag{13}
\end{equation*}
$$

The simplified scheme then becomes

$$
\begin{equation*}
2 X \underset{\beta}{\stackrel{\alpha}{\rightleftarrows}} Y+Z \tag{14}
\end{equation*}
$$

in which $\alpha$ and $\beta$ are apparent rate constants, which can be related to the true second-order rate constants $\alpha^{\prime}$ and $\beta^{\prime}$ via the expressions

$$
\begin{gather*}
X_{2}=\lambda X, \quad \lambda=1 /(1+\mu) \\
\alpha=\alpha^{\prime} \lambda^{2}, \quad \beta=\beta^{\prime} Z \tag{15}
\end{gather*}
$$

Because the label can occur to varying extents in chromate and bichromate, and to varying extents and locations in dichromate, several subspecies $X_{i}, Y_{i}$ of $X$ and $Y$ may be distinguished, and it is possible to follow their evolution via the rate constants $\alpha$ and $\beta .{ }^{19}$ (A comparable approach was used by Mills and Urey to follow ${ }^{18} \mathrm{O}$ incorporation into aqueous $\mathrm{H}_{2} \mathrm{CO}_{3} / \mathrm{CO}_{2}$ ). ${ }^{20}$ However, it is also possible to develop equations for the direct atom (fraction) transfer of O among $X, Y$, and $Z$. This approach is used here (when applied to the $\mathrm{H}_{2} \mathrm{CO}_{3} / \mathrm{CO}_{2} / \mathrm{H}_{2} \mathrm{O}$ system, it can be shown that this leads to the same rate equations as developed by Mills and Urey). ${ }^{21}$

A2. Equations of Chemical Evolution. As the isotopic decay processes depend on the concentrations $X$ and $Y$, it is essential to know the time dependences of these. The appropriate differential equations are

$$
\begin{gather*}
\dot{X}=2\left(\beta Y-\alpha X^{2}\right) \\
\dot{Y}=\alpha X^{2}-\beta Y \tag{16}
\end{gather*}
$$

Since $X+2 Y=X_{0}$ (starting with $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ at $t=0$ ), elimination gives

$$
\begin{equation*}
\dot{X}=-2 \alpha\left(X-a_{1}\right)\left(X+a_{2}\right) \tag{17}
\end{equation*}
$$

where

$$
\begin{align*}
& a_{1}=\left[\left(\beta^{2}+8 \alpha \beta X_{0}\right)^{1 / 2}-\beta\right] / 4 \alpha  \tag{18}\\
& a_{2}=\left[\left(\beta^{2}+8 \alpha \beta X_{0}\right)^{1 / 2}+\beta\right] / 4 \alpha
\end{align*}
$$

[^4]If we define a rate constant $\nu_{1}$ such that

$$
v_{1}=2 \alpha\left(a_{1}+a_{2}\right)=\left(\beta^{2}+8 \alpha \beta X_{0}\right)^{1 / 2}
$$

then the general solution to eq 17 is

$$
\begin{equation*}
X=\left(a_{1} C+a_{2} \mathrm{e}^{-\nu_{1} t}\right) /\left(C-\mathrm{e}^{-v_{1} t}\right) \tag{19}
\end{equation*}
$$

where $C$ is the constant of integration. Since $X=X_{0}$ when $t=$ 0 , then $C=\left(X_{0}+a_{2}\right) /\left(X_{0}-a_{1}\right)$. If $\alpha X_{0} / \beta \ll 1$, loss of significance may occur in the calculation of $a_{1}$ in eq 18. In such cases the approximation $C \cong\left(\beta / 2 \alpha X_{0}\right)^{2}$ is useful.

Equation 19 defines the time dependence of $X\left(\mathrm{CrO}_{4}{ }^{2-}+\right.$ $\mathrm{HCrO}_{4}{ }^{-}$) as chemical equilibrium is being established and approaches a single exponential near equilibrium. ${ }^{22}$ The first of eqs 18 guarantees $X_{0}>a_{1}$, and $X \rightarrow a_{1}$ as $t \rightarrow \infty$ Thus $a_{1}$ defines the equilibrium concentration of $X$. The time dependence of $Y$ follows from $Y=\left(X_{0}-X\right) / 2$.

A3. Equations of Isotopic Evolution. We begin with the following definitions: $p=$ atom fraction of label in $\mathrm{CrO}_{4}{ }^{2-}$ and $\mathrm{HCrO}_{4}^{-} ; q=$ atom fraction of label in $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-} ; r=$ atom fraction of label in $\mathrm{H}_{2} \mathrm{O}$.

$$
\begin{align*}
& U=\left[{ }^{17} \mathrm{O}\right]_{x}=4 p X \\
& V=\left[{ }^{17} \mathrm{O}\right]_{y}=7 q Y  \tag{20}\\
& W=\left[{ }^{17} \mathrm{O}\right]_{z}=r Z
\end{align*}
$$

in which $U, V$, and $W$ represent concentrations of isotopic label. It is these values which are of use in part $\mathbf{C}$.

The equations of isotopic evolution are ${ }^{23}$

$$
\begin{gather*}
\dot{U}=\beta(Y+W Y / Z)-2 \alpha U X \\
\dot{V}={ }^{7} /{ }_{4} \alpha \mathrm{UX}-\beta V  \tag{21}\\
\dot{W}={ }^{1}{ }_{4} \alpha U X-\beta W Y / Z
\end{gather*}
$$

These can be derived as follows using eqs 20 to eliminate $p, q$, and $r$. The rate of conversion of $X$ into $Y$ is $2 \alpha X^{2}$, so the rate of loss of label from $X$ is $4 p\left(2 \alpha X^{2}\right)=2 \alpha U X$. At the same time, label is returning to $X$ from $Y$ at a rate $7 q \beta Y=\beta V$, and from $Z$ at a rate $r \beta Y=\beta W Y / Z$. The first of eqs 21 follows. Similarly, label is being lost from $Y$ to $X$ at a rate $\beta V$. When calculating the rate at which label is being received by $Y$ from $W$, we have to take into account the fact that one oxygen atom (out of eight) is lost to solvent whenever a dichromate ion is formed. Thus the rate of transfer of label from $X$ to $Y$ is $7 p \alpha X^{2}=7 \alpha U X / 4$. The second of eqs 21 is now explained. Finally, the rate of loss of label from the water is $\beta W Y / Z$, and the rate of transfer of label from bichromate to water is $(1 / 8) 2 p \alpha X^{2}=\alpha U X / 4$. This accounts for the last of eqs 21.

Adding eqs 21 gives the expected conservation law $U+V$ $+W=U_{0}+W_{0} \cong U_{0} .{ }^{24}$

[^5]Table 1. Chemical Concentrations ( $X$ ), Isotopic Concentrations $(U)$, Isotopic Fractions ( $p$ ) for Monomeric $\mathrm{Cr}(\mathrm{VI})\left(\mathrm{CrO}_{4}{ }^{2-}+\right.$ $\mathrm{HCrO}_{4}^{-}$), and Isotopic Fractions for $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(q)$ and $\mathrm{H}_{2} \mathrm{O}(r)$ Calculated for O Exchange via the Dimerization Mechanism (Eq 1) at $\mathrm{pH}=3.00\left(\alpha=402.5 \mathrm{M}^{-1} \mathrm{~s}^{-1}, \beta=5.03 \mathrm{~s}^{-1} ; X_{0}=0.10 \mathrm{M}, p_{0}=\right.$ $\left.0.40 ; Y_{0}=0.00 \mathrm{M} ; Z_{0}=55.5 \mathrm{M}, r_{0}=0.037 \%\right), T=25^{\circ} \mathrm{C}$, and $I$ $=1.0 \mathrm{M}$

| $t / \mathrm{s}$ | $X / \mathrm{M}$ | $U / \mathrm{M}$ | $p$ | $p / q$ | $r$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0000 | 0.100 | 0.160 | 0.400 | 1.000 | 0.00037 |
| 0.0001 | 0.099 | 0.159 | 0.400 | 1.000 | 0.00037 |
| 0.0100 | 0.056 | 0.090 | 0.399 | 0.998 | 0.00053 |
| 0.0200 | 0.041 | 0.064 | 0.396 | 0.993 | 0.00060 |
| 0.0300 | 0.033 | 0.052 | 0.392 | 0.985 | 0.00063 |
| 0.0400 | 0.029 | 0.045 | 0.388 | 0.975 | 0.00066 |
| 0.0500 | 0.026 | 0.041 | 0.383 | 0.965 | 0.00068 |
| 0.0600 | 0.025 | 0.038 | 0.378 | 0.955 | 0.00070 |
| 0.0700 | 0.024 | 0.036 | 0.373 | 0.946 | 0.00071 |
| 0.0000 | 0.023 | 0.034 | 0.369 | 0.939 | 0.00073 |
| 0.0900 | 0.023 | 0.033 | 0.365 | 0.932 | 0.00074 |
| 0.1000 | 0.023 | 0.033 | 0.361 | 0.926 | 0.00076 |
| 0.20 | 0.022 | 0.030 | 0.337 | 0.904 | 0.00088 |
| 0.30 | 0.022 | 0.028 | 0.320 | 0.901 | 0.00100 |
| 0.40 | 0.022 | 0.027 | 0.304 | 0.901 | 0.00111 |
| 0.50 | 0.022 | 0.026 | 0.290 | 0.901 | 0.00121 |
| 0.60 | 0.022 | 0.024 | 0.275 | 0.901 | 0.00131 |
| 0.70 | 0.022 | 0.023 | 0.262 | 0.901 | 0.00141 |
| 0.80 | 0.022 | 0.022 | 0.249 | 0.900 | 0.00150 |
| 0.90 | 0.022 | 0.021 | 0.237 | 0.901 | 0.00158 |
| 1.00 | 0.022 | 0.020 | 0.226 | 0.901 | 0.00166 |
| 2 | 0.022 | 0.012 | 0.138 | 0.902 | 0.00228 |
| 2 | 0.022 | 0.007 | 0.084 | 0.903 | 0.00266 |
| 3 | 0.022 | 0.005 | 0.052 | 0.905 | 0.00288 |
| 4 | 0.022 | 0.003 | 0.033 | 0.909 | 0.00302 |
| 5 | 0.022 | 0.002 | 0.021 | 0.914 | 0.00310 |
| 6 | 0.022 | 0.001 | 0.014 | 0.921 | 0.00315 |
| 7 | 0.001 | 0.010 | 0.931 | 0.00318 |  |
| 8 | 0.022 | 0.022 | 0.001 | 0.007 | 0.942 |
| 9 | 0.022 | 0.00320 |  |  |  |
| 10 | 0.022 | 0.000 | 0.006 | 0.955 | 0.00321 |
| 20 | 0.022 | 0.000 | 0.003 | 0.999 | 0.00323 |
| 30 | 0.022 | 0.000 | 0.003 | 1.000 | 0.00323 |
| 40 | 0.022 | 0.000 | 0.003 | 1.000 | 0.00323 |
| 50 | 0.022 | 0.000 | 0.003 | 1.000 | 0.00323 |
|  |  |  |  |  |  |

Alternatively eqs 21 may be expressed in terms of atom fractions

$$
\begin{gather*}
\dot{p}=(\beta Y / 4 X)(7 q+r-8 p) \\
\dot{q}=\left(\alpha X^{2} / Y\right)(p-q)  \tag{22}\\
\dot{r}=\left(\alpha X^{2} p-\beta Y r\right) / Z
\end{gather*}
$$

Equations 21 hold at all times, but for evaluation purposes that for $\dot{q}$ in eq 22 requires a limit to be taken when $Y \rightarrow 0, t \rightarrow 0$.

A4. Numerical Evaluations of Isotopic Exchange. As stated above we can use exact solutions for $X$ and $Y$ (cf. section A2) to carry out numerical integrations of the nonlinear eqs 21 or 22. For $\dot{q}$ in eq 22 , we need to find the limit as $t \rightarrow 0$ and this can readily be done by expanding the variables in powers of $t$. The most relevant results are

$$
\begin{align*}
& p=p_{0}-p_{2} t^{2}-\ldots \\
& q=p_{0}-p_{2} t^{2 / 3}-\ldots \tag{23}
\end{align*}
$$

in which $p_{2}$ takes the value $\alpha \beta X_{0}\left(p_{0}-r_{0}\right) / 8$. Integration of system 22 and insertion into eqs 20 then leads to values of $U$, $V$, and $W$.

Numerical data for one set of conditions are listed in Table 1. It can be seen that $p$ and $q$ start from the same initial value $p_{0}$, but over time decrease, with $p$ diminishing more rapidly


Figure 1. Rates of loss of oxygen label (i.e., ${ }^{17} \mathrm{O}$ or ${ }^{18} \mathrm{O}$ ) from monomeric chromate into water (unlabeled) at three $\mathrm{pHs}(\mathrm{A}, 3.0$; B , 7.3; $\mathrm{C}, 9.0$ ) and four $\mathrm{Cr}(\mathrm{VI})$ concentrations [( ---$) 0.001 \mathrm{M}$, ( - ) $0.01 \mathrm{M},(---) 0.10 \mathrm{M}$, and (---) 2.0 M ] calculated assuming that exchange occurs via dimerization (eq 1). Rate constants ( $\alpha$ and $\beta$ ) are given in Table 1.
than $q$ at first. This results from the fact that in the forward dimerization reaction $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (and $\mathrm{H}_{2} \mathrm{O}$ ) is produced with the same fractional label as $\mathrm{HCrO}_{4}^{-}$, whereas in the reverse hydrolysis reaction solvent, with a lesser ${ }^{17} \mathrm{O}$ content, is introduced causing an immediate reduction in $p$. It can be shown that the $p / q$ ratio will never fall below the value $7 / 8$. Data for $U$ are shown graphically in Figure 1. The initial change in $U$ closely follows that for chemical change ( $X$ ), but because $p$ is also decreasing, slowly at first, the correspondence is never exact. Thus changes in isotopic concentration never parallel those for chemical change.

A5. Evaluation of Rate Constants for Isotopic Exchange. Isotopic equilibrium will normally be far from complete when chemical equilibrium has been established. Under this condition an isotopic imbalance between all three O-containing species

Table 2. Chemical and Isotopic Exchange Rate Constants

| $\mathrm{Cr}(\mathrm{VI}) / \mathrm{M}$ | pH | $\alpha^{a} / \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | $\beta^{c} / \mathrm{s}^{-1}$ | $\nu_{1} / \mathrm{s}^{-1}$ | $v_{2} / \mathrm{s}^{-1}$ | $v_{3} / \mathrm{s}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.001 | 3.0 | 402.5 | 5.03 | 6.44 | 5.66 | $7.82 \times 10^{-2}$ |
| 0.01 |  |  |  | 13.7 | 9.05 | 0.30 |
| 0.10 |  |  |  | 40.5 | 22.3 | 0.50 |
| 2.0 |  | $674{ }^{\text {b }}$ | 5.03 | 232 | 118 | 0.68 |
| 0.001 | 6.0 | 2.90 | 0.036 | $3.74 \times 10^{-2}$ | $3.66 \times 10^{-2}$ | $8.30 \times 10^{-5}$ |
| 0.01 |  |  |  | $4.78 \times 10^{-2}$ | $4.13 \times 10^{-2}$ | $6.44 \times 10^{-4}$ |
| 0.10 |  |  |  | 0.106 | $6.86 \times 10^{-2}$ | $2.30 \times 10^{-3}$ |
| 2.0 |  | $4.85{ }^{\text {b }}$ | 0.036 | 0.396 | 0.212 | $4.31 \times 10^{-3}$ |
| 0.001 | 7.3 | 2.52 | 0.032 | $3.20 \times 10^{-2}$ | $3.20 \times 10^{-2}$ | $4.14 \times 10^{-7}$ |
| 0.01 |  |  |  | $3.21 \times 10^{-2}$ | $3.20 \times 10^{-2}$ | $4.13 \times 10^{-6}$ |
| 0.10 |  |  |  | $3.27 \times 10^{-2}$ | $3.23 \times 10^{-2}$ | $4.09 \times 10^{-5}$ |
| 2.0 |  | $4.23{ }^{\text {b }}$ | 0.032 | $3.91 \times 10^{-2}$ | $3.51 \times 10^{-2}$ | $4.61 \times 10^{-4}$ |
| 0.001 | 9.0 | 3.50 | 0.0436 | $4.36 \times 10^{-2}$ | $4.36 \times 10^{-2}$ | $2.41 \times 10^{-10}$ |
| 0.01 |  |  |  | $4.36 \times 10^{-2}$ | $4.36 \times 10^{-2}$ | $2.41 \times 10^{-9}$ |
| 0.10 |  |  |  | $4.36 \times 10^{-2}$ | $4.36 \times 10^{-2}$ | $2.43 \times 10^{-8}$ |
| 2.0 |  | $5.86{ }^{\text {b }}$ | 0.0436 | $4.36 \times 10^{-2}$ | $4.36 \times 10^{-2}$ | $3.20 \times 10^{-7}$ |

${ }^{a} \alpha=2.5\left(4.0 \times 10^{5}\right) a_{\mathrm{H}^{+}}+\left(1.0 \times 10^{5}\right) a_{\mathrm{OH}^{-}} ; K_{\mathrm{d}}=80 \mathrm{M}^{-1}(I=1.0 \mathrm{M}) .{ }^{b} \alpha=4.185+\left(6.70 \times 10^{5}\right) a_{\mathrm{H}^{+}}+\left(1.69 \times 10^{5}\right) a_{\mathrm{OH}^{-}} ; K_{\mathrm{d}}=132 \mathrm{M}^{-1}$ $(I=6.0 \mathrm{M}) .{ }^{c} \beta=\alpha / K_{\mathrm{d}}$.
still exists, $q>p \gg r ; p$ and $q$ are normally still far from their equilibrium values, $p=q=r$.

Once chemical equilibrium has been established, $X$ and $Y$ become constant (values $a_{1}$ and $\alpha a_{1}{ }^{2} / \beta$, respectively; cf. section A2), making eqs 21 and 22 linear and homogeneous with constant coefficients; viz. for (22)

$$
\begin{gather*}
\dot{p}=\left(\alpha a_{1} / 4\right)(7 q+r-8 p) \\
\dot{q}=\beta(p-q)  \tag{24}\\
\dot{r}=\left(\alpha a_{1}^{2} / Z\right)(p-r)
\end{gather*}
$$

Standard matrix methods may then be applied for their solution. Equations 24 take the form $\dot{x}=\mathbf{A} x$, where

$$
\mathbf{A}=\left[\begin{array}{lll}
-8 A_{1} & 7 A_{1} & A_{1} \\
A_{2} & -A_{2} & 0 \\
A_{3} & 0 & -A_{3}
\end{array}\right]
$$

with $A_{1}=\alpha a_{1} / 4, A_{2}=\beta$, and $A_{3}=\alpha a_{1}^{2} / Z$. Their general solution, determined by the matrix coefficients, is

$$
\begin{equation*}
x=C_{1} \epsilon_{1}+C_{2} \epsilon_{2} \mathrm{e}^{-v_{2} t}+C_{3} \epsilon_{3} \mathrm{e}^{-v_{3} t} \tag{25}
\end{equation*}
$$

where $\nu_{2}$ and $\nu_{3}$ are negatives of the non-zero eigenvalues of $\mathbf{A}, \epsilon_{i}$ are the corresponding eigenvectors, and $C_{i}$ are the constants of integration (the eigenvalue corresponding to eigenvector $\epsilon_{1}$ can be shown to be 0 ). It is clear that there are two rates of isotopic evolution, with the rate constants $\nu_{2}$ and $\nu_{3}$ being solutions to the quadratic
$v^{2}-\left(8 A_{1}+A_{2}+A_{3}\right) v+\left(A_{1} A_{2}+A_{2} A_{3}+7 A_{1} A_{3}\right)=0$
We have chosen $\nu_{3}<\nu_{2}$ such that $\nu_{3}$ dominates at large $t$. Table 2 lists $v_{2}$ and $\nu_{3}$ values, as well as $\nu_{1}$ for chemical evolution, at four pH values and four $\mathrm{Cr}(\mathrm{VI})$ concentrations.

It can be seen that $v_{2}$ differs usefully from $v_{1}$ only at low pH and high $[\mathrm{Cr}(\mathrm{VI})]$. In part C of this paper, because of the experimental method employed, we will only be concerned with $v_{3}$. This is correctly represented by the McKay equation ${ }^{25}$

$$
\begin{equation*}
\left.\ln \left\{\left(\left[{ }^{17} \mathrm{O}\right]_{t}-\left[{ }^{17} \mathrm{O}\right]_{\infty}\right) /\left({ }^{[17} \mathrm{O}\right]_{0}-\left[{ }^{17} \mathrm{O}\right]_{\infty}\right)\right\}=-v_{3} t \tag{27}
\end{equation*}
$$

[^6]and dominates overall exchange at pH values $>7$. Table 2 shows $v_{3}$ to have a first-order dependence on [CrVI] at pH 9.0 and 7.3 (i.e., it represents a second-order rate constant) but is beginning to approach independence in $[\mathrm{Cr}(\mathrm{VI})]$ at pH 3.0 .
B. Equilibrium and Rate Constants. Early potentiometric $^{26-29}$ and spectrophotometric ${ }^{28,30}$ studies suggested the existence of monomeric $\mathrm{HCrO}_{4}^{-}$in neutral and acidic aqueous solution, and more recent measurements using similar methods have confirmed this. ${ }^{31-33}$ However its existence has also been disputed on the grounds that an absorption, expected at 880 $\mathrm{cm}^{-1}$ in the Raman spectrum, is not seen. ${ }^{34,35}$ This uncertainty has found its way into the recent review literature. ${ }^{36}$ In this section we give additional spectral evidence for the existence of $\mathrm{HCrO}_{4}^{-}$, and ${ }^{17} \mathrm{O}$ NMR data relating to its properties, as well as kinetic data for its conversion into $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(\alpha$ and $\beta$, eq 1$)$ under the conditions used in the O -exchange study (part C ).

B1. Properties of $\mathbf{H C r O}_{4}{ }^{-}$. Figure 2A gives the visible spectrum of a very dilute $\left(5.2 \times 10^{-2} \mathrm{mM}\right)$ solution of $\mathrm{Na}_{2}-$ $\mathrm{CrO}_{4}$ at pH 9.98 (a) and 3.05 (b), $I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}, 25^{\circ} \mathrm{C}$. The two clearly differ, but both obey Beer's Law over a 10fold concentration range about this concentration. At concentrations greater than 1 mM , Beer's law is still obeyed for the pH 9.98 data, but at pH 3.05 , Beer's law is not followed due to increasing polymerization (e.g., $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ formation). The 5.2 $\times 10^{-2} \mathrm{mM}$ spectrum shows a pH independence between 11.0 and 7.5 (Figure $2 \mathrm{~A}(\mathrm{a})$ ) and between 3.5 and 1.5 (Figure 2A(b)), but between pH 7.5 and 4.0 , titration with $1 \mathrm{M} \mathrm{HClO}_{4}$ (microliter additions) gave an excellent titration curve ( 370 nm , inset of Figure 2A) corresponding to the addition of one $\mathrm{H}^{+}$ per $\mathrm{Cr}(\mathrm{VI})$, giving $K_{\mathrm{a}}=(1.51 \pm 0.10) \times 10^{-6} \mathrm{M}\left(\mathrm{p} K_{\mathrm{a}}=5.82\right)$ under this $1.0 \mathrm{M} \mathrm{NaClO}_{4}$ condition $\left(25^{\circ} \mathrm{C}\right)$. Increasing the $\mathrm{Cr}-$ (VI) concentration by a factor of 4 gave an identical titration curve. Titration in $3 \mathrm{M} \mathrm{NaClO}_{4}$ gave $K_{\mathrm{a}}=(2.8 \pm 0.2) \times 10^{-6}$ $\mathrm{M}\left(\mathrm{p} K_{\mathrm{a}}=5.55\right)$ and in $6 \mathrm{M} \mathrm{NaClO}_{4} K_{\mathrm{a}}=(3.2 \pm 0.2) \times 10^{-6}$ $\mathrm{M}\left(\mathrm{p} K_{\mathrm{a}}=5.49\right)$. Such data demonstrate an electrolyte, but not a $\mathrm{Cr}(\mathrm{VI})$ concentration, dependence. Provided $\mathrm{CrO}_{4}{ }^{2-}$ is

[^7]

Figure 2. (A) Absorption spectra of $5.16 \times 10^{-2} \mathrm{mM} \mathrm{Cr}(\mathrm{VI})$ solutions (1.0 $\mathrm{M} \mathrm{NaClO}_{4}, 25^{\circ} \mathrm{C}$ ) at (a) $\mathrm{pH} 9.98\left(\epsilon_{374}=4570, \epsilon_{274}=3550\right)$, and (b) $\mathrm{pH} 3.05\left(\epsilon_{348}=1490, \epsilon_{257}=2010\right)$. Inset gives the pH titration curve. (B) Absorption spectra of acidified 0.208 mM solutions of Cr (VI) in (c) $\mathrm{H}_{2} \mathrm{O}$ and (d) $\mathrm{CH}_{3} \mathrm{CN}$ containing $2.5 \% \mathrm{H}_{2} \mathrm{O}$.
accepted as the species present in alkaline solution eq 28 follows:

$$
\begin{equation*}
\mathrm{CrO}_{4}^{2}+\mathrm{H}^{+} \rightleftharpoons \mathrm{HCrO}_{4}^{-}\left(1 / K_{\left.\mathrm{a}_{\left(\mathrm{HCrO}_{4}^{-}\right)}\right)}\right) \tag{28}
\end{equation*}
$$

A potentiometric titration ( $0.01 \mathrm{M} \mathrm{Cr}(\mathrm{VI}), 1.0 \mathrm{M}, \mathrm{NaClO}_{4}, 25$ ${ }^{\circ} \mathrm{C}$ ) also showed the addition of one $\mathrm{H}^{+}$per $\mathrm{Cr}(\mathrm{VI})$ centered at pH 5.72, ${ }^{37}$ but its $\mathrm{Cr}(\mathrm{VI})$ independence was not established and so distinction from dimerization reaction 1 was not proved. However, earlier potentiometric data by Sasaki ${ }^{31}$ obtained at low concentration ( $0.1,0.2 \mathrm{mM}$ ) clearly establish equilibrium 28 as the correct expression. Table 3 summarizes our $K_{\mathrm{a}}$ values and compares them with those in the literature.

Close examination of the pH 3.05 spectrum, Figure 2B(c) shows the presence of substructure in the near-UV (350-400 nm ), and this is more apparent when the spectrum is recorded in acetonitrile ( $2.5 \% \mathrm{H}_{2} \mathrm{O}$ ), Figure 2B(d). Such substructure can be attributed to vibrational bands caused by a change from $T_{\mathrm{d}}$ to $C_{3 v}$ symmetry. ${ }^{38}$ Similar spectra have been observed for other $\mathrm{CrO}_{3} \mathrm{X}^{-}$species $(\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}) .{ }^{39}$ It was outside the

[^8]Table 3. $\mathrm{p} K_{\mathrm{a}}$ and $K_{\mathrm{d}}$ Values $\left(25^{\circ} \mathrm{C}\right)^{a}$

| $\mathrm{p} K_{\mathrm{a}}{ }^{b}$ | $K_{\mathrm{d}} / \mathrm{M}^{-1 c}$ | ref |
| :--- | :---: | :--- |
| $5.82(\mathrm{~S})$ | 80 | this work |
|  | 107 | 48 |
|  | 77 | $57\left(0.5 \mathrm{M} \mathrm{NaClO}_{4}\right)$ |
| $5.55(\mathrm{~S})$ |  | this work $\left(3 \mathrm{M} \mathrm{NaClO}_{4}\right)$ |
| $5.89(\mathrm{~S}, \mathrm{P})$ |  | $31(3 \mathrm{M} \mathrm{NaClO})$ |
| $5.49(\mathrm{~S})$ | 132 | this work $\left(6 \mathrm{M} \mathrm{NaClO}_{4}\right)$ |
| $5.72(\mathrm{P})$ |  | this work |
| $5.80(\mathrm{~N})$ | 81 | this work |
| $5.76(\mathrm{P})$ | 67 | 33 |

${ }^{a} I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right)$ unless otherwise stated. ${ }^{b} \mathrm{~S}=$ spectrophotometric, $\mathrm{P}=$ potentiometric, $\mathrm{N}={ }^{17} \mathrm{O}$ NMR method. ${ }^{c} K_{\mathrm{d}}=\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right] /$ $\left[\mathrm{HCrO}_{4}{ }^{-}\right]^{2}$.


Figure 3. ${ }^{17} \mathrm{O} \mathrm{NMR}$ spectra (reference external, $\mathrm{MoO}_{4}{ }^{2-}, 529 \mathrm{ppm}$ ) of $(\mathrm{A}) 0.18 \mathrm{M} \mathrm{Cr}(\mathrm{VI})$ at pH 6.10 and $I=1.0 \mathrm{M}\left(\mathrm{NaCF}_{3} \mathrm{SO}_{3}\right)$ and (B) 2.00 M Cr(VI) at pH 5.83 and $I=6.0 \mathrm{M}$ (solvent enrichment $4 \%$ ). Signal assignments: (a) $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (terminal O), (b) $\mathrm{CrO}_{4}{ }^{2-}\left(+\mathrm{HCrO}_{4}^{-}\right)$, (c) $\mathrm{MoO}_{4}{ }^{2-}$, (d) $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (bridging O ).
scope of the present investigation to study this in detail, but the asymmetry of the $\mathrm{CrO}_{3}(\mathrm{OH})^{-}$ion (compared to $\mathrm{CrO}_{4}{ }^{2-}$ ) appears to be established.

Unlike visible spectral or potentiometric measurements, an ${ }^{17} \mathrm{O}$ NMR study gives more definitive information since the monomer and dimer can be seen as separate absorptions. Figure 3 gives two such spectra at $\mathrm{pH} \sim 6([\mathrm{Cr}(\mathrm{VI})]=0.18$ and 2.0 M) externally referenced to $\mathrm{MoO}_{4}{ }^{2-}(529 \mathrm{ppm})$. The $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ signals appear at 1115 ppm (terminal) and 335 ppm (bridging), intensity ratio $6: 1$, and the chemical shift and line width of the 1115 ppm signal was shown to be independent of $\mathrm{pH}(7.0-$ $3.0)$ and $\mathrm{Cr}(\mathrm{VI})$ concentration ( $0.02-0.32 \mathrm{M}$ ). This means that chemical exchange broadening as suggested by Figgis and coworkers ${ }^{8}$ (eq 6) and $\mathrm{H}^{+}$-catalyzed hydrolysis of $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ as observed by Jackson and Taube ${ }^{40}$ are not important rate processes under these conditions. However the $\mathrm{CrO}_{4}{ }^{2-} / \mathrm{HCrO}_{4}^{-}$ absorption ( $820-860 \mathrm{ppm}$ ) does show a pH dependence moving to lower frequencies and broadening as the pH is decreased. The field shift can be related to protonation, and line broadening, to $T_{1}$ and $T_{2}$ relaxation in the $\mathrm{HCrO}_{4}^{-}$ion. The latter aspect has been discussed in detail elsewhere. ${ }^{41}$ No additional absorptions were seen up to $2.0 \mathrm{M} \mathrm{Cr}(\mathrm{VI})$ so that other species, such as $\mathrm{Cr}_{3} \mathrm{O}_{10}{ }^{2-}$, are not present in significant amounts under these conditions.

The chemical shift in the $\mathrm{CrO}_{4}{ }^{2-} / \mathrm{HCrO}_{4}^{-}$absorption (820$860 \mathrm{ppm})$ was used to determine the acidity constant of $\mathrm{HCrO}_{4}^{-}$.

[^9]

Figure 4. ${ }^{17} \mathrm{O}$ NMR spectra for a solution 0.025 M in $\mathrm{Cr}(\mathrm{VI})$ and $I=$ $1.0 \mathrm{M}\left(\mathrm{NaCF}_{3} \mathrm{SO}_{3}\right)$ in $35 \% \mathrm{H}_{2}{ }^{17} \mathrm{O}$ : (A) $\mathrm{pH}=7.05$; (B) $\mathrm{pH}=6.05$; (C) $\mathrm{pH}=5.58$ (the peak at $\sim 970 \mathrm{ppm}$ arises from folding back of the water signal). Signal assignments: (a) $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (terminal O), (b) $\mathrm{CrO}_{4}{ }^{2-}$ $+\mathrm{HCrO}_{4}{ }^{-}$, (c) $\mathrm{MoO}_{4}{ }^{2-}$.

Two titrations with $\mathrm{CF}_{3} \mathrm{SO}_{3} \mathrm{H}$ were carried out, the first using $0.32 \mathrm{M} \mathrm{Na}_{2} \mathrm{CrO}_{4}$ in $5 \%{ }^{17} \mathrm{O}$-enriched $\mathrm{H}_{2} \mathrm{O}(I=1.0 \mathrm{M})$ and the second using $0.025 \mathrm{M} \mathrm{Na}_{2} \mathrm{CrO}_{4}$ in $35 \%{ }^{17} \mathrm{O}$-enriched $\mathrm{H}_{2} \mathrm{O}(I=$ 1.0 M with $\left.\mathrm{NaCF}_{3} \mathrm{SO}_{3}\right)$. Three representative spectra from the second titration are shown in Figure 4, and Table 4 gives more extensive data (cf. supporting information). The observed chemical shift ( $\delta_{\text {obs }}$ ) represents the weighted average for $\mathrm{CrO}_{4}{ }^{2-}$ $\left(\delta_{\mathrm{CrO}_{4}}{ }^{2-}\right)$ and $\mathrm{HCrO}_{4}^{-}\left(\delta_{\mathrm{HCrO}_{4}-}\right)$, viz.

$$
\begin{equation*}
\delta_{\mathrm{obs}}=f_{\mathrm{CrO}_{4}{ }^{2-}} \delta_{\mathrm{CrO}_{4}{ }^{2-}}+f_{\mathrm{HCrO}_{4}-} \delta_{\mathrm{HCrO}_{4}{ }^{-}} \tag{29}
\end{equation*}
$$

( $f_{\mathrm{CrO}_{4}{ }^{2-}}$ and $f_{\mathrm{HCrO}_{4}}{ }^{-}$represent mole fractions). Incorporation into equilibrium 28 leads to

$$
\begin{equation*}
\delta_{\mathrm{obs}}=\left(\delta_{\mathrm{HCrO}_{4}^{-}} a_{\mathrm{H}^{+}}+\delta_{\mathrm{CrO}_{4}^{2-}} K_{\mathrm{a}}\right) /\left(K_{\mathrm{a}}+a_{\mathrm{H}^{+}}\right) \tag{30}
\end{equation*}
$$

in which all quantities except $K_{\mathrm{a}}$ and $\delta_{\mathrm{HCrO}_{4}-}$ are known $\left(\delta_{\mathrm{CrO}_{4}}{ }^{2-}\right.$ $=812 \mathrm{ppm}$ was taken as the average of two observations at high pH ). It was not possible to observe directly the $\mathrm{HCrO}_{4}^{-}$ ion $\left(\delta_{\mathrm{HCrO}_{4}-}\right)$ since the signal broadened into the baseline at pH values $<5$. Fitting the data to eq $30^{42}$ gave $K_{\mathrm{a}}=1.58 \times 10^{-6} \mathrm{M}$ $\left(\mathrm{p} K_{\mathrm{a}}=5.80\right)$ and $\delta_{\mathrm{HCrO}_{4-}}=860 \mathrm{ppm}$. This $K_{\mathrm{a}}$ value agrees well with the spectrophotometric value (Table 3).

Information relating to the number of oxygen atoms in $\mathrm{HCrO}_{4}^{-}$can also be obtained from the areas of the $\mathrm{Cr}(\mathrm{VI})$
signals at $[\mathrm{Cr}]_{\mathrm{T}}=0.025 \mathrm{M}$ (Figure 4) provided it is accepted that $\mathrm{CrO}_{4}{ }^{2-}$ contains four, ${ }^{43}$ and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ seven, O atoms. Table 5 lists signal areas obtained at three pH values. The total area (column 4), allowing for the one O atom lost from $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ to $\mathrm{H}_{2} \mathrm{O}$, is essentially constant. If $\mathrm{HCrO}_{4}^{-}$were present as $\mathrm{H}_{3} \mathrm{CrO}_{5}^{-}$(i.e., as five-coordinate $\mathrm{CrO}_{3}(\mathrm{OH})\left(\mathrm{OH}_{2}\right)^{-}$), then the combined total area of the pH 5.58 absorptions would be 85.8 units (at this pH some $36 \%$ of the combined signal area represents $\mathrm{HCrO}_{4}^{-}$). Within the accuracy of the integration ( $\pm 5 \%$ over the three measurements), the observed total area falls short of this and remains invariant at the three acidities. It is therefore concluded that $\mathrm{HCrO}_{4}{ }^{-}$is properly represented as containing four bound O atoms.

B2. Dimerization Constant $\left(K_{d}\right)$ and Dimerization Rates ( $\alpha$ and $\boldsymbol{\beta}$ ). The separate ${ }^{17} \mathrm{O}$ absorptions provide a direct measure of $K_{\mathrm{d}}\left(K_{\mathrm{d}}=\left[\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}\right] /\left[\mathrm{HCrO}_{4}^{-}\right]^{2}\right)$ once $K_{\mathrm{a}}$ is known. Integration of the $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ and combined monomer $\left(\mathrm{CrO}_{4}{ }^{2-}+\right.$ $\mathrm{HCrO}_{4}^{-}$) signals was carried out at four pH values following titration of $0.18 \mathrm{M} \mathrm{Na}_{2} \mathrm{CrO}_{4}$ with $2 \mathrm{M} \mathrm{CF}_{3} \mathrm{SO}_{3} \mathrm{H}$ in $5 \% \mathrm{H}_{2}{ }^{17} \mathrm{O}$. These data (Table 6, supporting information) give an average $K_{\mathrm{d}}$ value of $81 \pm 5 \mathrm{M}^{-1}$ at $I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right)$ and a value of $132 \mathrm{M}^{-1}$ for the one measurement at $I=6.0 \mathrm{M}\left(\mathrm{Na}_{2} \mathrm{SO}_{4}\right)$. The former value agrees well with the spectrophotometric value ( 80 $\mathrm{M}^{-1}$, Table 3), and the latter compares with a reported value of $133 \mathrm{M}^{-1}$ in $3.0 \mathrm{M} \mathrm{NaClO}_{4} .{ }^{44}$

Let us now examine the dimerization rates since, in order to compare the observed rates of O exchange (part C) with those calculated from the dimerization equilibrium, it is necessary to know $\alpha$ and $\beta$ under the same conditions. Forward and reverse rates are given by ${ }^{45}$

$$
\begin{gather*}
R_{\mathrm{f}}=\alpha\left[\mathrm{HCrO}_{4}{ }^{-}\right]^{2} \\
R_{\mathrm{r}}=\beta\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right] \tag{31}
\end{gather*}
$$

with $\alpha$ and $\beta$ containing both acid ${ }^{46}$ and base ${ }^{47}$ contributions, viz.

$$
\begin{gather*}
\alpha=k_{1}+k_{2} a_{\mathrm{H}^{+}}+k_{3} a_{\mathrm{OH}^{-}}+k_{4}[\mathrm{~B}]+k_{5}[\mathrm{HA}] \\
\beta=k_{-1}+k_{-2} a_{\mathrm{H}^{+}}+k_{-3} a_{\mathrm{OH}^{-}}+k_{-4}[\mathrm{~B}]+k_{-5}[\mathrm{HA}] \tag{32}
\end{gather*}
$$

Activation parameters $\left(\Delta H^{\ddagger},{ }^{48} \Delta S^{\ddagger},{ }^{49}\right.$ and $\left.\Delta V^{\ddagger 50}\right)$ have been obtained for some of these pathways.

Rate data ( $k_{\mathrm{obs}}$ ) for the approach to equilibrium in acid solution ( $\mathrm{pH} 2-3$ ) were obtained by rapidly mixing $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ and $\mathrm{HClO}_{4}$ solutions and following the absorbance change on a stopped-flow spectrophotometer. Under this condition only the $\mathrm{H}^{+}$-catalyzed pathway is important, ${ }^{48-51}$ viz. $\alpha=k_{2} a_{\mathrm{H}^{+}}$and $\beta=k_{-2} a_{\mathrm{H}^{+}}$, and variation in the observed first-order rate

[^10]Table 5. ${ }^{17} \mathrm{O}$ NMR Results ${ }^{a}$ [Analysis of Peak Areas in Figure $\left.4\left([\mathrm{Cr}(\mathrm{VI})]=0.025 \mathrm{M} ; I=1.0 \mathrm{M}\left(\mathrm{NaCF}_{3} \mathrm{SO}_{3}\right) ; 25^{\circ} \mathrm{C}\right)\right]$

| pH | $\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}^{-}$ |  | $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ |  |  | total area | $\frac{\left(\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}^{-}\right)}{\%(\text { area })_{\mathrm{obs}^{\mathrm{d}}}{ }^{\mathrm{a}}}$ | $\frac{\left(\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}^{-}\right)}{\%(\text { area })_{\mathrm{calc}^{e}}{ }^{e}}$ | $\% \mathrm{HCrO}_{4}{ }^{-f}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ppm | (area) ${ }_{\text {obs }}{ }^{\text {b }}$ | $\mathrm{ppm}^{\text {c }}$ | (area) ${ }_{\text {obs }}{ }^{\text {b }}$ | (area) ${ }_{\text {obs }} \times 8 / 6^{\text {c }}$ |  |  |  |  |
| 7.05 | 817 | 75.1 |  | 0 | 0 | 75.1 | 100 | 99 | 5.0 |
| 6.05 | 832 | 54.7 | 1115 | 14.7 | 19.6 | 74.3 | 73.6 | 77.2 | 37 |
| 5.58 | 842 | 46.3 | 1115 | 24.1 | 32.1 | 78.4 | 59.1 | 60.6 | 63.5 |

${ }^{a}$ Areas obtained by instrument integration (average of three); arbitrary units. ${ }^{b}$ Observed area corrected using standard (external) $\mathrm{MoO}_{4}{ }^{2-}$ absorption. ${ }^{c}$ Terminal O absorption. The factor $8 / 6$ allows for loss of one oxygen to solvent and one to bridging oxygen ( 335 ppm signal not shown) on forming $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ from two $\mathrm{HCrO}_{4}{ }^{-}$units. ${ }^{d}$ Observed $\%$ area $\left(\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}{ }^{-}\right)$. ${ }^{e}$ Calculated $\%$ area $\left(\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}{ }^{-}\right)$based on $\mathrm{p} K_{\mathrm{a}}=5.82$, $K_{\mathrm{d}}=80 \mathrm{M}^{-1}$, and four O atoms in both $\mathrm{CrO}_{4}{ }^{2-}$ and $\mathrm{HCrO}_{4}{ }^{-}$, i.e. $\% ~(\text { area })_{\text {calc }}=100\left(4\left[\mathrm{CrO}_{4}{ }^{2-}\right]+4\left[\mathrm{HCrO}_{4}-{ }^{-}\right]\right) /\left(4\left[\mathrm{CrO}_{4}{ }^{2-}\right]+4\left[\mathrm{HCrO}_{4}{ }^{-}\right]+6\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right]\right)$. $[\mathrm{Cr}]_{\mathrm{T}}=\left[\mathrm{CrO}_{4}{ }^{2-}\right]+\left[\mathrm{HCrO}_{4}^{-}\right]+2\left[\mathrm{Cr}_{2} \mathrm{O}_{7^{2-}}{ }^{-}\right]=0.025 \mathrm{M} .{ }^{f}$ Calculated $\% \mathrm{HCrO}_{4}{ }^{-}$in $\left(\mathrm{CrO}_{4}{ }^{2-}+\mathrm{HCrO}_{4}{ }^{-}\right)$absorption, based on $\mathrm{p} K_{\mathrm{a}}=5.82$.
constant is given by

$$
\begin{equation*}
k_{\mathrm{obs}}=k_{-2} a_{\mathrm{H}^{+}}+4 k_{2} a_{\mathrm{H}^{+}}\left[\mathrm{HCrO}_{4}^{-}\right] \tag{33}
\end{equation*}
$$

$\left[\mathrm{HCrO}_{4}^{-}\right]$can be expressed as
$\left[\mathrm{HCrO}_{4}{ }^{-}\right]=\left(-1+\left(1+8\left(k_{2} / k_{-2}\right)\left[\mathrm{Cr}_{\mathrm{T}}\right]^{1 / 2}\right) / 4\left(k_{2} / k_{-2}\right)\right.$
where $\left[\mathrm{Cr}_{\mathrm{T}}\right]$ represents the total chromium concentration (i.e., $\left[\mathrm{Cr}_{\mathrm{T}}\right]=2\left[\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}\right]+\left[\mathrm{HCrO}_{4}^{-}\right]$). Rate data (Table 7, supporting information) were fitted to eqs 33 and 34 giving $k_{2}=$ $4.01 \times 10^{5} \mathrm{M}^{-2} \mathrm{~s}^{-1}, k_{-2}=5.04 \times 10^{3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, and $K_{\mathrm{d}}=$ $k_{2} / k_{-2}=80 \mathrm{M}^{-1}$. The $k_{2}$ and $k_{-2}$ values are in reasonable agreement with those of Pladziewicz and Espenson, ${ }^{48}$ obtained under similar conditions ( $1 \mathrm{M} \mathrm{LiClO}_{4}, k_{2}=6.33 \times 10^{5} \mathrm{M}^{-2}$ $\left.\mathrm{s}^{-1}, k_{-2}=6.35 \times 10^{3} \mathrm{M}^{-1} \mathrm{~s}^{-1}\right)$.

The reaction in neutral solution ( $\mathrm{pH} 6-7$ ) also contains contributions from the spontaneous pathways $k_{1}$ and $k_{-1}$ so that $\alpha=k_{1}+k_{2} a_{\mathrm{H}^{+}}$and $\beta=k_{-1}+k_{-2} a_{\mathrm{H}^{+}}$. Under this condition the approach to equilibrium is a relaxation process ${ }^{22}$ with firstorder rate constants given by

$$
\begin{equation*}
k_{\mathrm{obs}}=k_{-1}+k_{-2} a_{\mathrm{H}^{+}}+4\left(k_{1}+k_{2} a_{\mathrm{H}^{+}}\right)\left[\mathrm{HCrO}_{4}^{-}\right] \tag{35}
\end{equation*}
$$

where

$$
\begin{array}{r}
{\left[\mathrm{HCrO}_{4}^{-}\right]=\left(-\left(1+K_{\mathrm{a}} / a_{\mathrm{H}^{+}}\right)+\left(\left(1+K_{\mathrm{a}} / a_{\mathrm{H}^{+}}\right)^{2}+\right.\right.} \\
\left.\left.8 K_{\mathrm{d}}\left[\mathrm{Cr}_{\mathrm{T}}\right]\right)^{1 / 2}\right) / 4 K_{\mathrm{d}} \tag{36}
\end{array}
$$

$\left(\left[\mathrm{Cr}_{\mathrm{T}}\right]=\left[\mathrm{CrO}_{4}{ }^{2-}\right]+\left[\mathrm{HCrO}_{4}^{-}\right]+2\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right]\right)$. Rate data under these conditions were obtained by mixing $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ and $\mathrm{Na}_{2}-$ $\mathrm{Cr}_{2} \mathrm{O}_{7}$ plus indicator solutions and following the absorbance increase due to the indicator. The wavelength chosen depended on the indicator used, and this in turn depended on the solution pH . Table 8 lists data (supporting information), and the best fit to eqs 35 and 36 was obtained using $k_{1}=2.4 \mathrm{M}^{-1} \mathrm{~s}^{-1}$ and $k_{-1}=0.030 \mathrm{~s}^{-1}$.

In alkaline solution only the hydrolysis term $k_{-3} a_{\mathrm{OH}}-$ is important. This takes on a value of $1.26 \times 10^{3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, (c.f. Table 9, supporting information).

Buffers were used in the O-exchange experiments to maintain pH , and it was necessary to determine their contribution to eqs 32. These data are rather extensive and are given in their entirety elsewhere. ${ }^{37}$ Direct nucleophilic catalysis in the hydrolysis of $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ has been reported for TRIS ${ }^{52}$ and $\mathrm{HPO}_{4}{ }^{2-} .53$ Table 10 summarizes rate constants for buffer catalysis; these are used in part C below.
(52) Brasch, N. E.; Buckingham, D. A.; Clark, C. R. Inorg. Chem. 1994, 33, 2683.
(53) Brasch, N. E.; Buckingham, D. A.; Clark, C. R. Aust. J. Chem. 1994, 47, 2283.

Table 10. Rate Constants $\left(k_{-4}\right)$ for Buffer-Catalyzed Hydrolysis of $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\left(I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right), 25^{\circ} \mathrm{C}\right)$

| buffer | buffer $\mathrm{p} K_{\mathrm{a}}{ }^{a}$ | $k_{4} / \mathrm{M}^{-1} \mathrm{~s}^{-1}$ |
| :--- | :---: | :---: |
| CAPS | 10.57 | 76 |
| CHES | $9.59^{b}$ | 47 |
| DABCO | 9.29 | $4.35 \times 10^{3}$ |
| TAPS | 8.45 | 3.0 |
| TRIS | $8.23^{b}$ | 55 |
| TES | 7.56 | 1.2 |
| BES | 7.26 | 0.53 |
| BISTRIS | 6.85 | 0.022 |
| MES | 6.36 | 0.82 |
| $\mathrm{HPO}_{4}{ }^{2-}$ | $6.13^{b}$ | 24 |

${ }^{a}$ Taken as the pH of a half-neutralized solution. ${ }^{b}$ Determined by potentiometric titration.


Figure 5. First-order plot of loss of ${ }^{17} \mathrm{O}$ label from $\mathrm{Cr}(\mathrm{VI})(0.0272 \mathrm{M}$, $40 \%{ }^{17} \mathrm{O}$ enriched) into $\mathrm{H}_{2} \mathrm{O}$ at pH 7.39 (TES buffer, 0.10 M ) and 25 ${ }^{\circ} \mathrm{C}\left(I=1.0, \mathrm{NaClO}_{4}\right)$.
C. ${ }^{17} \mathrm{O}$ Exchange. Two mechanisms for oxygen exchange are likely. Exchange can either be direct via routes such as those given in Scheme 1 (and analogous paths involving $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ ), or it can occur via the dimerization process expressed by eq 1 (a combination of the two is also possible). The two mechanisms give rates of exchange having different $\mathrm{Cr}(\mathrm{VI})$ and pH dependencies. In this section we use the observed rate constants for dimerization ( $\alpha$ and $\beta$, part B ) to calculate the rates of O exchange via this pathway ( $\nu_{3}$, eq 26) and compare these with observed rates of ${ }^{17} \mathrm{O}$ exchange. We then discuss the mechanism.

C1. Rates at Low $\mathbf{C r}(\mathrm{VI})$ Concentrations ( $<0.15 \mathrm{M}$ ), $I=$ 1.0 M. When ${ }^{17} \mathrm{O}$-enriched $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ is dissolved in normal water, decay of the chromate signal coincides with an increase in the height of the $\mathrm{H}_{2} \mathrm{O}$ signal. For $40 \%{ }^{17} \mathrm{O}$ enrichments and $[\mathrm{Cr}(\mathrm{VI})]>0.15 \mathrm{M}$, the former peak does not decay to zero due to significant ${ }^{17} \mathrm{O}$ concentrations at equilibrium, but at lower $[\mathrm{Cr}(\mathrm{VI})]$, it disappears into the background after approximately three half-lives. Figure 5 gives a plot of $\ln \left(h_{\mathrm{t}}\right)$ versus time for exchange at pH 7.39 and $[\mathrm{Cr}(\mathrm{VI})]=0.0272 \mathrm{M}$ with the linear


Figure 6. Plot of $\log k_{\text {obs }}$ versus pH for loss of ${ }^{17} \mathrm{O}$ label from $\mathrm{Cr}(\mathrm{VI})$ ( $0.01-0.152 \mathrm{M}, 40 \%{ }^{17} \mathrm{O}$ enriched) into $\mathrm{H}_{2} \mathrm{O}, 25{ }^{\circ} \mathrm{C}, I=1.0 \mathrm{M}$ $\left(\mathrm{NaClO}_{4}\right)$.

## Scheme 1

$$
\begin{aligned}
& \mathrm{Cr} \mathrm{O}_{4}{ }^{-}+\mathrm{H}_{2} \mathrm{O} \xrightarrow{\mathrm{k}_{1}^{\prime}} \mathrm{CrO}_{3} \mathrm{O}^{2-}+\mathrm{H}_{2} \mathrm{O} \\
& +\mathrm{H}^{+} \\
& K_{a(2)} \|^{\|} \\
& \mathrm{HCr}^{\bullet} \bullet_{4}{ }^{-}+\mathrm{H}_{2} \mathrm{O} \xrightarrow{\mathrm{k}_{2}^{\prime}} \mathrm{HCr} \bullet_{3} \mathrm{O}^{-}+\mathrm{H}_{2} \bullet \\
& +\mathrm{H}^{+} \\
& \mathrm{K}_{\mathrm{a}(1)} \| \text {, } \\
& \mathrm{H}_{2} \mathrm{Cr}_{4}+\mathrm{H}_{2} \mathrm{O} \xrightarrow{\mathrm{k}_{3}^{\prime}} \mathrm{H}_{2} \mathrm{Cr}_{3} \mathrm{O}+\mathrm{H}_{2} \text { - }
\end{aligned}
$$

correspondence showing that the reaction is first-order, $k_{\mathrm{obs}}=$ $7.75 \times 10^{-4} \mathrm{~s}^{-1}$. Similar first-order plots were obtained for all exchanges irrespective of $\mathrm{Cr}(\mathrm{VI})$ concentration, buffer condition, and pH .

First-order rate data ( $k_{\mathrm{obs}}$ ) are listed in Table 11. Before considering their pH dependence it is important to mention that $k_{\mathrm{obs}}$ is independent of $\mathrm{Cr}(\mathrm{VI})$ concentration and buffer concentration. This, observation is important when making decisions concerning the mechanism. The pH dependence is plotted in Figure 6. Two lines are drawn to show the two main dependencies. The slope of 2.0 suggests that for $\mathrm{pH}<8 \mathrm{a}$ close to second-order dependence on $\left[\mathrm{H}^{+}\right]$holds. The horizontal line for data above pH 10 suggests that $k_{\text {obs }}$ is pH independent under such conditions. Closer examination however shows that the data do not agree exactly with these slopes, especially below pH 7 , where a less than second-order dependence is seen, and in the pH region $8-10$, where $k_{\text {obs }}$ is larger than expected. The former suggests that protonation to form $\mathrm{HCrO}_{4}^{-}\left(\mathrm{p} K_{\mathrm{a}}=5.80\right)$ is reducing the pH dependence below pH 7 , and the latter suggests that there is a term first-order in $\left[\mathrm{H}^{+}\right]$which contributes in the $\mathrm{pH} 8-10$ region.

Table 11 also gives $\alpha$ and $\beta$ values for the various buffer and pH conditions employed in the O -exchange measurements (columns 4 and 5), and rates of exchange calculated assuming the dimerization mechanism is responsible ( $v_{3}$, column 6). Comparison with $k_{\text {obs }}$ (column 7) shows no agreement. This is especially significant for the low-pH data where $v_{3}$ is some 100 times smaller than $k_{\text {obs }}$. Furthermore, $v_{3}$ shows a buffer dependence whereas $k_{\mathrm{obs}}$ does not. Dimerization $\left(v_{3}\right)$ must contribute to O exchange, but clearly is not a major pathway.

Following Okumura, ${ }^{9}$ we attribute the major pathways for exchange to direct exchange into $\mathrm{CrO}_{4}{ }^{2-}\left(k_{1}{ }^{\prime}\right), \mathrm{HCrO}_{4}{ }^{-}\left(k_{2}{ }^{\prime}\right)$,
and $\mathrm{H}_{2} \mathrm{CrO}_{4}\left(k_{3}{ }^{\prime}\right)$. Scheme 1 leads to the expression
$k_{\mathrm{calc}}=\left(k_{1}{ }^{\prime} K_{\mathrm{a}(2)}+k_{2}{ }^{\prime} a_{\mathrm{H}^{+}}+k_{3}{ }^{\prime} a_{\mathrm{H}^{+}}^{2} / K_{\mathrm{a}(1)}\right) /\left(K_{\mathrm{a}(2)}+a_{\mathrm{H}^{+}}\right)$
where $K_{\mathrm{a}(1)}$ represents the acidity constant for $\mathrm{H}_{2} \mathrm{CrO}_{4}$ and $K_{\mathrm{a}(2)}$ that for $\mathrm{HCrO}_{4}^{-}$(5.80). The final column of Table 11 gives the least-squares fit to the observed data resulting in $k_{1}{ }^{\prime}, k_{2}{ }^{\prime}$, and $k_{3}{ }^{\prime} / K_{\mathrm{a}(1)}$ values of $1.0 \times 10^{-6} \mathrm{~s}^{-1}, 1.05 \times 10^{-2} \mathrm{~s}^{-1}$, and 5.8 $\times 10^{5} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, respectively, under the $I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right)$, $25{ }^{\circ} \mathrm{C}$, condition. Assuming that $K_{\mathrm{a}(1)}=4.1 \mathrm{M},{ }^{54} k_{3}{ }^{\prime}$ takes on the value $2.4 \times 10^{6} \mathrm{~s}^{-1}$. Clearly the effects of protonating $\mathrm{CrO}_{4}{ }^{2-}$ are appreciable.

C2. Rates at Concentrations of $\mathbf{C r}(\mathrm{VI})$ up to $2.0 \mathrm{M}, I=$ 6.0 M. Like Okumura ${ }^{9}$ we also found that for pH values $<$ 7.5 the rate of O exchange increases with $\mathrm{Cr}(\mathrm{VI})$ concentration above $\sim 0.1 \mathrm{M}$. Under this condition significant amounts of $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ are present. Figure 7 gives one such plot at $[\mathrm{Cr}(\mathrm{VI})]$ $=2.0 \mathrm{M}(\mathrm{pH} 7.26)$, where $t_{1 / 2}$ for exchange is 2.4 min . This is to be compared with $t_{1 / 2} \sim 10.5 \mathrm{~min}$ for $[\mathrm{Cr}(\mathrm{VI})]=0.02 \mathrm{M}$ at the same pH . Table 12 gives $k_{\mathrm{obs}}$ values (column 6) for the concentration range $2.0-0.02 \mathrm{M} . \mathrm{Na}_{2} \mathrm{SO}_{4}$ was used as the supporting electrolyte to keep both the ionic strength ( $I=6.0$ M) and $\left[\mathrm{Na}^{+}\right]$constant. ${ }^{55}$ Difficulties were experienced in measuring pH for these solutions (due to subsequent crystallization of $\mathrm{Na}_{2} \mathrm{SO}_{4}$ in the NMR tube), so that while good reproducibility in rate was achieved for a particular solution $\left[\mathrm{H}^{+}\right]$was less certain. Using measured $K_{\mathrm{a}}$ and $K_{\mathrm{d}}$ values in 6 $\mathrm{M} \mathrm{NaClO}_{4}$ (Table 3), rates for the dimerization mechanism ( $v_{3}$, eq 26) were calculated, and these are listed in column 5. Once again it can be seen that dimerization does not account for the increase in exchange rate; it contributes only a maximum of $\sim 10 \%$ under the 2.0 M condition. Direct exchange into $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ is therefore suggested, ${ }^{56}$ Scheme 2, and this leads to the expression

$$
\begin{array}{r}
k_{\mathrm{calc}}=\left(k_{3}{ }^{\prime} a_{\mathrm{H}^{+}}^{2} / K_{\mathrm{a}(1)}+k_{4}^{\prime} K_{\mathrm{d}}\left[\mathrm{HCrO}_{4}^{-}\right] a_{\mathrm{H}^{+}}\right) /\left(K_{\mathrm{a}(2)}+\right. \\
a_{\mathrm{H}^{+}}\left(1+K_{\mathrm{d}}\left[\mathrm{HCrO}_{4}^{-}\right]\right) \tag{38}
\end{array}
$$

with exchange at lower pH being almost entirely via the $k_{3}{ }^{\prime}$ pathway (for $\mathrm{H}_{2} \mathrm{CrO}_{4}$, cf. Scheme 1) and via the unassisted exchange into $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\left(k_{4}{ }^{\prime}\right)$. The final column of Table 12 gives the least-square fit to the observed data, resulting in $k_{3}{ }^{\prime} / K_{\mathrm{a}(1)}$ and $k_{4}^{\prime}$ values of $1.2 \times 10^{6} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ and $3.8 \times 10^{-2} \mathrm{~s}^{-1}$, respectively. The former is within a factor of 2 of the value in $1.0 \mathrm{M} \mathrm{NaClO}_{4}$. The latter corresponds to spontaneous exchange into $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$, and its value is similar to that for unassisted hydrolysis $\left(k_{-1}=0.030 \mathrm{~s}^{-1}\right)$. Thus cleavage of the terminal and bridging $\mathrm{Cr}-\mathrm{O}$ bonds appear to be equally likely. This is represented by the concerted transition state $\mathbf{1}$ with bonds to


1


2


3
the bridging and terminal O atoms undergoing cleavage.

[^11]Table 11. Observed and Calculated Rate Constants for ${ }^{17} \mathrm{O}$ Exchange at Low $\mathrm{Cr}(\mathrm{VI})$ Concentrations ( $<0.152 \mathrm{M}$ ) $\left(I=1.0 \mathrm{M}\left(\mathrm{NaClO}_{4}\right), 25\right.$ ${ }^{\circ} \mathrm{C}$ )

| pH | $10^{2}[\mathrm{Cr}(\mathrm{VI})] / \mathrm{M}$ | $[B]_{\mathrm{T}} / \mathrm{M}$ | $\alpha^{a} / \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | $10^{2} \beta^{b} / \mathrm{s}^{-1}$ | $\nu_{3} / \mathrm{s}^{-1}$ | $k_{\text {obs }} / \mathrm{s}^{-1}$ | $k_{\text {calc }} / / /^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6.38 | 2.7 | 0.20 MES | 2.8 | 3.5 | $4.9 \times 10^{-4}$ | $5.3 \times 10^{-2}$ | $5.2 \times 10^{-2}$ |
| 6.59 | 2.7 | 0.20 BISTRIS | 2.6 | 3.3 | $2.2 \times 10^{-4}$ | $2.2 \times 10^{-2}$ | $2.2 \times 10^{-2}$ |
| 6.71 | 8.5 | 0.20 BISTRIS | 2.6 | 3.3 | $4.0 \times 10^{-4}$ | $1.2 \times 10^{-2}$ | $1.3 \times 10^{-2}$ |
| 6.82 | 15.2 | 0.20 BISTRIS | 2.6 | 3.3 | $4.4 \times 10^{-4}$ | $8.55 \times 10^{-3}$ | $8.5 \times 10^{-3}$ |
| 7.08 | 1.5 | 0.20 BES | 2.6 | 3.3 | $1.7 \times 10^{-5}$ | $2.9 \times 10^{-3}$ | $2.9 \times 10^{-3}$ |
| 7.09 | 1.6 | 0.20 BES | 2.6 | 3.3 | $1.7 \times 10^{-3}$ | $3.0 \times 10^{-3}$ | $2.8 \times 10^{-3}$ |
| 7.10 | 2.7 | 0.20 BES | 2.6 | 3.3 | $2.8 \times 10^{-5}$ | $3.55 \times 10^{-3}$ | $2.7 \times 10^{-3}$ |
| 7.11 | 2.6 | 0.20 BES | 2.6 | 3.3 | $2.6 \times 10^{-5}$ | $3.6 \times 10^{-3}$ | $2.6 \times 10^{-3}$ |
| 7.28 | 1.3 | 0.20 TES | 2.6 | 3.3 | $6.1 \times 10^{-6}$ | $1.3 \times 10^{-3}$ | $1.3 \times 10^{-3}$ |
| 7.29 | 2.8 | 0.20 TES | 2.6 | 3.3 | $1.25 \times 10^{-5}$ | $1.3 \times 10^{-3}$ | $1.2 \times 10^{-3}$ |
| 7.33 | 9.0 | 0.20 TES | 2.6 | 3.3 | $3.3 \times 10^{-5}$ | $1.0 \times 10^{-3}$ | $1.1 \times 10^{-3}$ |
| 7.39 | 2.7 | 0.10 TES | 2.6 | 3.3 | $7.75 \times 10^{-6}$ | $7.75 \times 10^{-4}$ | $8.5 \times 10^{-4}$ |
| 7.40 | 2.7 | 0.20 TES | 2.6 | 3.3 | $7.4 \times 10^{-6}$ | $7.5 \times 10^{-4}$ | $8.1 \times 10^{-4}$ |
| 7.41 | 2.7 |  | 2.5 | 3.1 | $6.8 \times 10^{-6}$ | $8.1 \times 10^{-4}$ | $7.8 \times 10^{-4}$ |
| 7.47 | 5.4 | 0.20 TES | 2.6 | 3.3 | $1.1 \times 10^{-5}$ | $6.2 \times 10^{-4}$ | $6.3 \times 10^{-4}$ |
| 8.06 | 1.0 | 0.20 TAPS | 2.8 | 3.5 | $1.5 \times 10^{-7}$ | $7.4 \times 10^{-5}$ | $8.4 \times 10^{-5}$ |
| 8.07 | 2.7 | 0.20 TAPS | 2.8 | 3.5 | $3.8 \times 10^{-7}$ | $7.0 \times 10^{-5}$ | $8.2 \times 10^{-5}$ |
| 8.19 | 2.6 | 0.133 TES | 2.8 | 3.5 | $2.1 \times 10^{-7}$ | $5.3 \times 10^{-5}$ | $5.85 \times 10^{-5}$ |
| 8.33 | 1.1 | 0.200 TAPS | 3.0 | 3.8 | $5.0 \times 10^{-8}$ | $2.5 \times 10^{-5}$ | $4.0 \times 10^{-5}$ |
| 8.34 | 1.1 | 0.20 TAPS | 3.2 | 4.0 | $2.0 \times 10^{-8}$ | $1.5 \times 10^{-5}$ | $2.3 \times 10^{-5}$ |
| 8.57 | 2.5 | 0.267 TAPS | 3.3 | 4.1 | $4.1 \times 10^{-8}$ | $1.7 \times 10^{-5}$ | $2.1 \times 10^{-5}$ |
| 9.03 | 3.0 | 0.20 CHES | 5.6 | 7.0 | $1.0 \times 10^{-8}$ | $7.7 \times 10^{-6}$ | $7.4 \times 10^{-6}$ |
| 9.12 | 1.2 | 0.40 TAPS | 4.8 | 6.0 | $2.3 \times 10^{-9}$ | $6.9 \times 10^{-6}$ | $6.2 \times 10^{-6}$ |
| 9.50 | 2.6 | 0.20 CHES | 9.9 | 12.4 | $1.8 \times 10^{-9}$ | $3.8 \times 10^{-6}$ | $3.1 \times 10^{-6}$ |
| 9.99 | 2.6 | 0.20 CHES | 19.1 | 23.9 | $3.6 \times 10^{-10}$ | $3.3 \times 10^{-6}$ | $1.7 \times 10^{-6}$ |
| 11.08 | 2.6 | 0.20 CAPS | 136 | $1.7 \times 10^{2}$ | $1.7 \times 10^{-11}$ | $3.0 \times 10^{-6}$ | $1.05 \times 10^{-6}$ |
| 12.00 | 2.8 |  | $1.01 \times 10^{3}$ | $1.26 \times 10^{3}$ | $2.0 \times 10^{-12}$ | $1.0 \times 10^{-6}$ | $1.0 \times 10^{-6}$ |
| 13.00 | 2.7 |  | $1.01 \times 10^{4}$ | $1.26 \times 10^{4}$ | $1.9 \times 10^{-13}$ | $9.1 \times 10^{-7}$ | $1.0 \times 10^{-6}$ |

${ }^{a} \alpha=k_{1}+k_{2} a_{\mathrm{H}^{+}}+k_{3} a_{\mathrm{OH}^{-}}+k_{4}[\mathrm{~B}]$ using $k_{1}=2.5 \mathrm{M}^{-1} \mathrm{~s}^{-1}, k_{2}=4.0 \times 10^{5} \mathrm{M}^{-2} \mathrm{~s}^{-1}, k_{3}=1.01 \times 10^{5} \mathrm{M}^{-2} \mathrm{~s}^{-1}$, and $k_{4}=80 k_{-4}\left(k_{-4}\right.$, Table 10). ${ }^{b} \beta=k_{-1}+k_{-2} a_{\mathrm{H}^{+}}+k_{-3} a_{\mathrm{OH}^{-}}+k_{-4}[\mathrm{~B}]$ using $k_{-1}=0.031 \mathrm{~s}^{-1}, k_{-2}=5.0 \times 10^{3} \mathrm{M}^{-1} \mathrm{~s}^{-1} ; k_{-3}=1.26 \times 10^{3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, and $k_{-4}$ values, Table $10 .^{c} v_{3}$ calculated using eq 26 and listed $\alpha$ and $\beta$ values. ${ }^{d}$ Calculated using eq 37 and $k_{1}{ }^{\prime}=1.0 \times 10^{-6} \mathrm{~s}^{-1}, k_{2}{ }^{\prime}=1.05 \times 10^{-2} \mathrm{~s}^{-1}, k_{3}{ }^{\prime} / K_{\mathrm{a}(1)}=5.8 \times 10^{5}$ $\mathrm{M}^{-1} \mathrm{~s}^{-1}$, and $K_{\mathrm{a}(2)}=1.6 \times 10^{-6} \mathrm{M}$.


Figure 7. ${ }^{17} \mathrm{O}$ NMR spectra showing progressive loss of label from $2.0 \mathrm{M} \mathrm{Cr}(\mathrm{VI})\left(16 \mathrm{mg}\right.$ of $\mathrm{Na}_{2} \mathrm{CrO}_{4}, 40 \%{ }^{17} \mathrm{O}$ enriched) to $\mathrm{H}_{2} \mathrm{O}$ at pH 7.26 and $25^{\circ} \mathrm{C}, I=6.0 \mathrm{M}$ (referenced to external $\mathrm{MoO}_{4}{ }^{2-}$ at 529 ppm , signal at right).

Likewise, cyclic transition states 2 and $\mathbf{3}$ are used for concerted exchange into $\mathrm{HCrO}_{4}^{-}$and $\mathrm{H}_{2} \mathrm{CrO}_{4}$ with H-bonding to the solvent being an important feature. Such additionelimination processes are supported by a recent study on $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$ in which rate-limiting addition of $\mathrm{HPO}_{4}{ }^{2-}$ has been interpreted in terms of formation of a transient five- (or six-) coordinate $\mathrm{Cr}(\mathrm{VI})$ intermediate. ${ }^{53}$

C3. Comparisons with Other Substitutions on $\mathbf{C r}(\mathrm{VI})$. This study substantiates Okumura's earlier ${ }^{18} \mathrm{O}$ study ${ }^{9}$ that solvent O exchange into monomeric $\mathrm{CrO}_{4}{ }^{2-}, \mathrm{HCrO}_{4}^{-}$, and $\mathrm{H}_{2}-$

## Scheme 2


$\mathrm{CrO}_{4}$ occurs directly. Our rate constants are $1.0 \times 10^{-6} \mathrm{~s}^{-1}$, $1.05 \times 10^{-2}$, and $2.4 \times 10^{6} \mathrm{~s}^{-1}$, respectively, for the three monomeric species. By converting these to a per O basis and expressing them as second-order rate constants (c.f Scheme 1), these take on values of $7.2 \times 10^{-8}, 7.6 \times 10^{-4}$, and $1.7 \times 10^{5}$ $\mathrm{M}^{-1} \mathrm{~s}^{-1}$. Likewise, solvent exchange into $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ on a per O basis has a rate constant of $4 \times 10^{-3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$. Table 13 compares these values with other known nucleophilic substitutions at $\mathrm{Cr}(\mathrm{VI})$. Two general observations can be made: (1) $\mathrm{H}_{2} \mathrm{O}$, and $\mathrm{CrO}_{4}{ }^{2-}$ in the dimerization reaction, are poor nucleophiles compared to the others and (2) the charge on the nucleophile is important. Thus $\mathrm{HCrO}_{4}{ }^{-}$is better than $\mathrm{CrO}_{4}{ }^{2-}$, but so too is $\left(\mathrm{NH}_{3}\right)_{5} \mathrm{CoOH}^{2+}$ compared to $\left(\mathrm{NH}_{3}\right)_{5} \mathrm{CoOH}_{2}{ }^{3+}$; $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$is the reactive phosphate species with $\mathrm{HCrO}_{4}^{-}$, whereas $\mathrm{HPO}_{4}{ }^{2-}$ reacts more rapidly with $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$. Such features are likely to be important in biological oxidation processes using $\mathrm{Cr}(\mathrm{VI})$, and we will now be turning our attention to a study of these.

## Experimental Section

Apparatus and Reagents. Spectrophotometric measurements were carried out using Cary 219 and Durrum D110 stopped-flow spectrophotometers. ${ }^{17} \mathrm{O}$ NMR spectra were recorded using a Varian VXRS 300 MHz spectrometer, operating at 40.662 MHz with a Varian coaxial 10 mm thermostated $\left(25^{\circ} \mathrm{C}\right)$ probe. Samples were contained in 10 mm NMR tubes with an external 5 mm aqueous ${ }^{17} \mathrm{O}$-enriched $\mathrm{Na}_{2}-$

Table 12. Observed and Calculated Rate Constants for ${ }^{17} \mathrm{O}$ Exchange at Variable $\mathrm{Cr}(\mathrm{VI})$ Concentrations $\left.\left(I=6.0 \mathrm{M}\left(\mathrm{Na}_{2} \mathrm{SO}\right)_{4}\right), 25{ }^{\circ} \mathrm{C}\right)$

| [Cr(VI)]/M | pH | $10^{4}\left[\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right] / \mathrm{M}$ | $10^{4}\left[\mathrm{HCrO}_{4}{ }^{-}\right] / \mathrm{M}$ | $10^{6} v_{3}{ }^{a} / \mathrm{s}^{-1}$ | $10^{4} k_{\text {obs }} / \mathrm{s}^{-1}$ | $10^{4}\left(k_{\text {obs }}-v_{3}\right) / \mathrm{s}^{-1}$ | $10^{4} k^{\text {calc }} / \mathrm{s}^{-1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.0 | 7.26 | 1190 | 297 | 521 | 48 | 43 | 29 |
| 2.0 | 7.59 | 321 | 154 | 125 | 11 | 9.85 | 7.3 |
| 2.0 | 7.79 | 134 | 99.5 | 52 | 4.4 | 3.9 | 3.0 |
| 1.0 | 7.15 | 510 | 194 | 400 | 36.5 | 32.5 | 34 |
| 1.0 | 7.16 | 492 | 191 | 400 | 36 | 32 | 32 |
| 0.50 | 7.15 | 141 | 102 | 220 | 30 | 28 | 27 |
| 0.20 | 7.27 | 14.3 | 32.5 | 86 | 15 | 14 | 12.5 |
| 0.10 | 7.26 | 3.8 | 16.6 | 29.4 | 12 | 11.5 | 12.4 |
| 0.060 | 7.27 | 1.31 | 9.96 | 17.0 | 10.5 | 10.3 | 11.4 |
| 0.040 | 7.30 | 0.51 | 6.15 | 9.90 | 9.1 | 9.0 | 9.8 |
| 0.020 | 7.32 | 0.117 | 2.94 | 4.53 | 9.1 | 9.05 | 8.8 |

${ }^{a}$ Calculated using eq 26 with $\alpha=4.18 \mathrm{M}^{-1} \mathrm{~s}^{-1}$ and $\beta=0.031 \mathrm{~s}^{-1} .{ }^{b}$ Calculated using eq 38 with $k_{3}{ }^{\prime} / K_{\mathrm{a}(1)}=1.2 \times 10^{6} \mathrm{M}^{-1} \mathrm{~s}^{-1}, K_{\mathrm{a}(2)}=3.2 \times$ $10^{-6} \mathrm{M}, K_{\mathrm{d}}=132 \mathrm{M}^{-1}$, and $k_{4}=3.8 \times 10^{-2} \mathrm{~s}^{-1}$.

Table 13. Second-Order Rate Constants for Substitution into $\mathrm{HCrO}_{4}^{-}$and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\left(I=1.0 \mathrm{M}, 25^{\circ} \mathrm{C}\right)$

| $\mathrm{HCrO}_{4}^{-}+\mathrm{Y} \rightarrow$ |  |  | $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}+\mathrm{Y} \rightarrow$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Y | $k / \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | ref | Y | $k / \mathrm{M}^{-1} \mathrm{~s}^{-1}$ | ref |
| $\mathrm{H}_{2} \mathrm{O}$ | $8 \times 10^{-4}$ | $a$ | $\mathrm{H}_{2} \mathrm{O}$ | $4 \times 10^{-3}$ | $a$ |
| $\mathrm{CrO}_{4}{ }^{2-}$ | $5.3 \times 10^{-4}$ | $a$ | $\mathrm{HPO}_{4}{ }^{2-}$ | 24 | 53 |
| $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$ | 1.05 | 53 | TRIS | 55 | 52 |
| $\mathrm{HCrO}_{4}^{-}$ | 2.4 | $a$ |  |  |  |
| $\left(\mathrm{NH}_{3}\right)_{5} \mathrm{CoOH}_{2}{ }^{3+}$ | 2.5 | 57 |  |  |  |
| $\left(\mathrm{NH}_{3}\right)_{5} \mathrm{CoOH}^{2+}$ | 242 | 57 |  |  |  |
| $\mathrm{HS}_{2} \mathrm{O}_{3}{ }^{-}$ | $2 \times 10^{4}$ | 58 |  |  |  |

## ${ }^{a}$ This work.

$\mathrm{MoO}_{4} / \mathrm{D}_{2} \mathrm{O}$ reference and lock $\left(\delta^{17} \mathrm{O}=529 \mathrm{ppm}\right)$ or external 5 mm $\mathrm{D}_{2} \mathrm{O} / \mathrm{DCl}$ lock. The former reference was prepared by adding a few drops of ${ }^{17} \mathrm{O}$-enriched $\mathrm{H}_{2} \mathrm{O}$ to a saturated solution of $\mathrm{Na}_{2} \mathrm{MoO}_{4}$ in $\mathrm{D}_{2} \mathrm{O}$ $\left(0.7 \mathrm{~cm}^{3}\right)$. Spectra were obtained using the standard Varian 1D pulse sequence with an acquisition time of 0.15 s , a delay of 0.05 s , a $90^{\circ}$ pulse angle, and a spectral window of $10^{5} \mathrm{~Hz}$. The pulse repetition time was sufficient to allow complete relaxation of the ${ }^{17} \mathrm{O}$ nuclei.

Solution pH was measured using a PHM 62 standard pH meter equipped with either G2020B/K4040 electrodes or an Ingold 6030-02 pH electrode designed to fit inside the NMR tube. Both electrodes were standardized using $0.025 \mathrm{M} \mathrm{Na}_{2} \mathrm{HPO}_{4} / 0.025 \mathrm{M} \mathrm{KH}_{2} \mathrm{PO}_{4}(\mathrm{pH}(25$ $\left.\left.{ }^{\circ} \mathrm{C}\right)=6.86\right)$ and either borax buffer $\left(0.01 \mathrm{M}, \mathrm{pH}\left(25^{\circ} \mathrm{C}\right)=9.18\right)$ or potassium hydrogen phthalate $\left(0.05 \mathrm{M}, \mathrm{pH}\left(25^{\circ} \mathrm{C}\right)=4.01\right)$. Measurements on alkaline solutions were carried out under a nitrogen atmosphere.
${ }^{17} \mathrm{O}$-labeled $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ was prepared by dissolving $\sim 1 \mathrm{~g}$ of $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ (AR, recrystallized, dried) in $2 \mathrm{~cm}^{3}$ of 40 atom $\% \mathrm{H}_{2}{ }^{17} \mathrm{O}$ (Yeda; this material also contained $\sim 35 \%{ }^{18} \mathrm{O}$ ), with equilibration for 2 weeks at $\sim 40{ }^{\circ} \mathrm{C}$. Enriched water was subsequently recovered on the vacuum line.

Acidity $\left(K_{\mathrm{a}}\right)$ and Equilibrium $\left(K_{\mathrm{d}}\right)$ Constants. Spectrophotometric Titration. An $8.33 \times 10^{-3} \mathrm{M}$ solution of $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ was made up in $1.0,3.0$, and $6.0 \mathrm{M} \mathrm{NaClO}_{4}$, adjusted to pH 2.5 , filtered, and diluted to give $2.08 \times 10^{-5} \mathrm{M}$ solutions. The pH was then successively altered over the range $2.5-10.0$ by microliter additions of 1 M NaOH , the pH recorded $\left(25^{\circ} \mathrm{C}\right)$, and the absorbance at 370 nm measured.

Potentiometric Titration. A $40.00 \mathrm{~cm}^{3}$ volume of $0.0100 \mathrm{M} \mathrm{Na}_{2}-$ $\mathrm{CrO}_{4}\left(I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ was titrated with 0.10 and $0.20 \mathrm{~cm}^{3}$ aliquots of $0.203 \mathrm{M} \mathrm{HClO}_{4}\left(I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ at $25^{\circ} \mathrm{C}$. The pH was recorded after each addition.
${ }^{17} \mathrm{O}$ NMR Titration. (a) 11.71 mg of $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ and 0.404 g of $\mathrm{NaCF}_{3} \mathrm{SO}_{3}$ were dissolved in $\sim 40 \%{ }^{17} \mathrm{O}$-labeled $\mathrm{H}_{2} \mathrm{O}$ (total volume 2.7 $\left.\mathrm{cm}^{3},\left[\mathrm{Cr}_{\mathrm{T}}\right]=0.025 \mathrm{M},\left[\mathrm{CF}_{3} \mathrm{SO}_{3}^{-}\right]=0.87 \mathrm{M}\right)$. This was transferred to the NMR tube and titrated stepwise with microliter additions of $\sim 5 \mathrm{M}$ $\mathrm{CF}_{3} \mathrm{SO}_{3} \mathrm{H}$. After each addition the pH was measured and the ${ }^{17} \mathrm{O}$ spectrum recorded. The pH was remeasured before the next addition of $\mathrm{CF}_{3} \mathrm{SO}_{3} \mathrm{H}$. (b) 76 mg of $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ and 0.21 g of $\mathrm{NaCF}_{3} \mathrm{SO}_{3}$ were dissolved in $35 \%{ }^{17} \mathrm{O}$-labeled $\mathrm{H}_{2} \mathrm{O}$ (total volume $2.6 \mathrm{~cm}^{3},\left[\mathrm{Cr}_{\mathrm{T}}\right]=0.18$ $\mathrm{M},\left[\mathrm{CF}_{3} \mathrm{SO}_{3}{ }^{-}\right]=0.46 \mathrm{M}$ ) and treated as above. (c) 0.135 g of $\mathrm{Na}_{2}{ }^{-}$ $\mathrm{CrO}_{4}(0.32 \mathrm{M})$ was dissolved in $5 \%{ }^{17} \mathrm{O}$-labeled $\mathrm{H}_{2} \mathrm{O}$ to give a total volume of $2.6 \mathrm{~cm}^{3}\left(\left[\mathrm{Cr}_{\mathrm{T}}\right]=0.32 \mathrm{M}\right)$ and treated as above.

For the measurement of $K_{\mathrm{d}}, \mathrm{Na}_{2} \mathrm{CrO}_{4}(81 \mathrm{mg})$ and 0.172 g of $\mathrm{NaCF}_{3}-$ $\mathrm{SO}_{3}$ or 0.546 g of $\mathrm{Na}_{2} \mathrm{SO}_{4}$ were dissolved in $2.5 \mathrm{~cm}^{3}$ of $5 \%{ }^{17} \mathrm{O}$-labeled $\mathrm{H}_{2} \mathrm{O}(I=1.0 \mathrm{M}, 6.0 \mathrm{M}$, respectively) and the pH adjusted to 6.52 , $6.10,6.04,5.74$, or 5.83 using microliter additions of $2 \mathrm{M} \mathrm{CF}_{3} \mathrm{SO}_{3} \mathrm{H}$.

Spectrophotometric Rate Measurements ( $\alpha$ and $\boldsymbol{\beta}$ ). Rate data for the uncatalyzed reaction were obtained by mixing $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ solutions ( $0.0333-0.133 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}$ ) with equal volumes of $\mathrm{Na}_{2^{-}}$ $\mathrm{Cr}_{2} \mathrm{O}_{7}$ solutions ( $0.0167-0.0667 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}$ ) containing indicator $\left(2.0 \times 10^{-5} \mathrm{M}\right.$, phenol red, chlorophenol red, or bromothymol blue) at $25^{\circ} \mathrm{C}$ in the Durrum. The resulting change in absorbance ( 557,575 , or 620 nm , respectively) was monitored as a function of time. Absorbance versus time data in acidic solution were obtained in a similar manner by mixing a $1.66 \times 10^{-4}$ to $6.66 \times 10^{-3} \mathrm{M} \mathrm{Na}_{2} \mathrm{CrO}_{4}$ solution $\left(I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ with $0.005-0.020 \mathrm{M} \mathrm{HClO}_{4}(I=1.0$ $\mathrm{M}, \mathrm{NaClO}_{4}$ ) at 385,400 , or 416 nm . Data in alkaline solutions were recorded after mixing $\mathrm{Na}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ solutions $\left(1.17 \times 10^{-3} \mathrm{M}, I=1.0 \mathrm{M}\right.$, $\mathrm{NaClO}_{4}$ ) and NaOH solutions $\left(0.033-0.100 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right.$ ) at 450 nm , while data in the presence of buffers were obtained after mixing $\mathrm{Na}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ solutions $\left(1.00 \times 10^{-3}\right.$ to $4.167 \times 10^{-3} \mathrm{M}, I=1.0$ $\mathrm{M}, \mathrm{NaClO}_{4}$ ) with buffers $\left(0.05-0.20 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ at $450-$ 480 nm . All data were collected using an OLIS 3820 stopped-flow data collection system in conjunction with a Northstar Horizon computer interfaced to the Durrum spectrophotometer. Data were treated using the OLIS nonlinear least-squares fitting routine Versatile Data Fit. Approach to equilibrium was first-order in all cases. For each experiment a separate solution was made up by mixing equal volumes of the two reagents and the pH recorded.

Oxygen Exchange Measurements. Solutions for exchange reactions with half-lives greater than $\sim 55 \mathrm{~s}$ were prepared by dissolving ${ }^{17}$ O-enriched $\mathrm{Na}_{2} \mathrm{CrO}_{4}(4.0-11.0 \mathrm{mg})$, normal unenriched $\mathrm{Na}_{2} \mathrm{CrO}_{4}(0-$ 0.79 g ), and $\mathrm{NaClO}_{4}$ or $\mathrm{Na}_{2} \mathrm{SO}_{4}$ (if necessary) in $2.5 \mathrm{~cm}^{3}$ of $\mathrm{H}_{2} \mathrm{O}$, or buffer solutions ( $0.133-0.40 \mathrm{M}$; MES, BISTRIS, BES, TES, TAPS, CHES, CAPS; $\left.I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ or $\mathrm{NaOH}\left(1.00 \times 10^{-2}\right.$ or $1.00 \times$ $10^{-1} \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}$ ). The pH was adjusted (concentrated $\mathrm{HClO}_{4}$ ) and the solution transferred to the 10 mm diameter NMR tube. Thermal equilibration in the spectrometer was carried out for about 2 min prior to data collection. More rapid exchange required that the separate components were thermostated $\left(25^{\circ} \mathrm{C}\right)$ before mixing. Reactions for which the half-lives were less than 12 h remained in the NMR probe during data collection. For reactions with longer halflives the solutions were capped and stored in a constant-temperature bath ( $25{ }^{\circ} \mathrm{C}$ ) between data collections. For rapidly exchanging conditions $\left(t_{1 / 2}<55 \mathrm{~s}\right)$ a quenching procedure was used. $\mathrm{Na}_{2} \mathrm{CrO}_{4}$ solutions containing $\mathrm{NaOH}\left(0.10 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}\right)$ were mixed with an appropriate buffer solution (BISTRIS, MES), and the reaction quenched at various times by adding an equal volume of NaOH solution ( $0.20 \mathrm{M}, I=1.0 \mathrm{M}, \mathrm{NaClO}_{4}$ ). NMR spectra were recorded shortly afterwards.

Difficulties were initially experienced in obtaining reproducible exchange data for $\mathrm{pH}>9$. Duplicate measurements differed by as much as $400 \%$. Previous investigators have considered the possibility of glass catalysis, ${ }^{59}$ and we found that the problem disappeared when Teflon containers were used. Thus, all CHES, CAPS, and NaOH

[^12]solutions were made up and immediately transferred to capped Teflon containers for storage. ${ }^{17} \mathrm{O}$ NMR exchange data were obtained using Teflon-lined NMR tubes under this condition.

It was not found necessary to use integrated peak areas as a measure of the ${ }^{17} \mathrm{O}$ concentration as the peak shape was constant for each experiment. When integrated areas were used these gave the same results as those obtained using peak heights. For slow exchanges (i.e., $t_{1 / 2}>10 \mathrm{~h}$ ), an external ${ }^{17} \mathrm{O}$ reference of $\mathrm{Na}_{2} \mathrm{MoO}_{4}(529 \mathrm{ppm})$ was used. In such cases relative peak heights were used; i.e., $\ln \left(h_{\mathrm{t}} / h_{\mathrm{r}}-\right.$ $h_{\infty} / h_{\mathrm{r}}$ ) versus time plots, where $h_{\mathrm{r}}$ represents the height of the $\mathrm{Mo}^{17} \mathrm{O}_{4}{ }^{2-}$ signal.

Errors. pH measurements were estimated to have an error of $\pm 0.02-0.04$ units (depending on electrode system) which corresponds to an error of $5-10 \%$ in $a_{\mathrm{H}^{+}}$. First-order rate constants (stopped-flow) are estimated to have an error of $3 \%$, while derived second-order rate
constants $\left(k=k_{\mathrm{obs}} /[X]\right)$ are estimated to have an error of 5-10\%. Firstorder rate constants obtained by ${ }^{17} \mathrm{O}$ NMR spectroscopy are estimated to have an error of $5-10 \%$ depending on the signal to noise ratio and line width. Integrated areas are estimated to have a maximum error of $5 \%$.

Supporting Information Available: Tables 4 and 6-9 containing ${ }^{17} \mathrm{O}$ chemical shift data for $\mathrm{p} K_{\mathrm{a}}\left(\mathrm{HCrO}_{4}{ }^{-}\right)$and $K_{\mathrm{d}}$ determinations and rate constants for the acid, neutral, and alkaline equilibration or hydrolysis of $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$, respectively (5 pages). See any current masthead page for ordering and Internet access instructions.

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